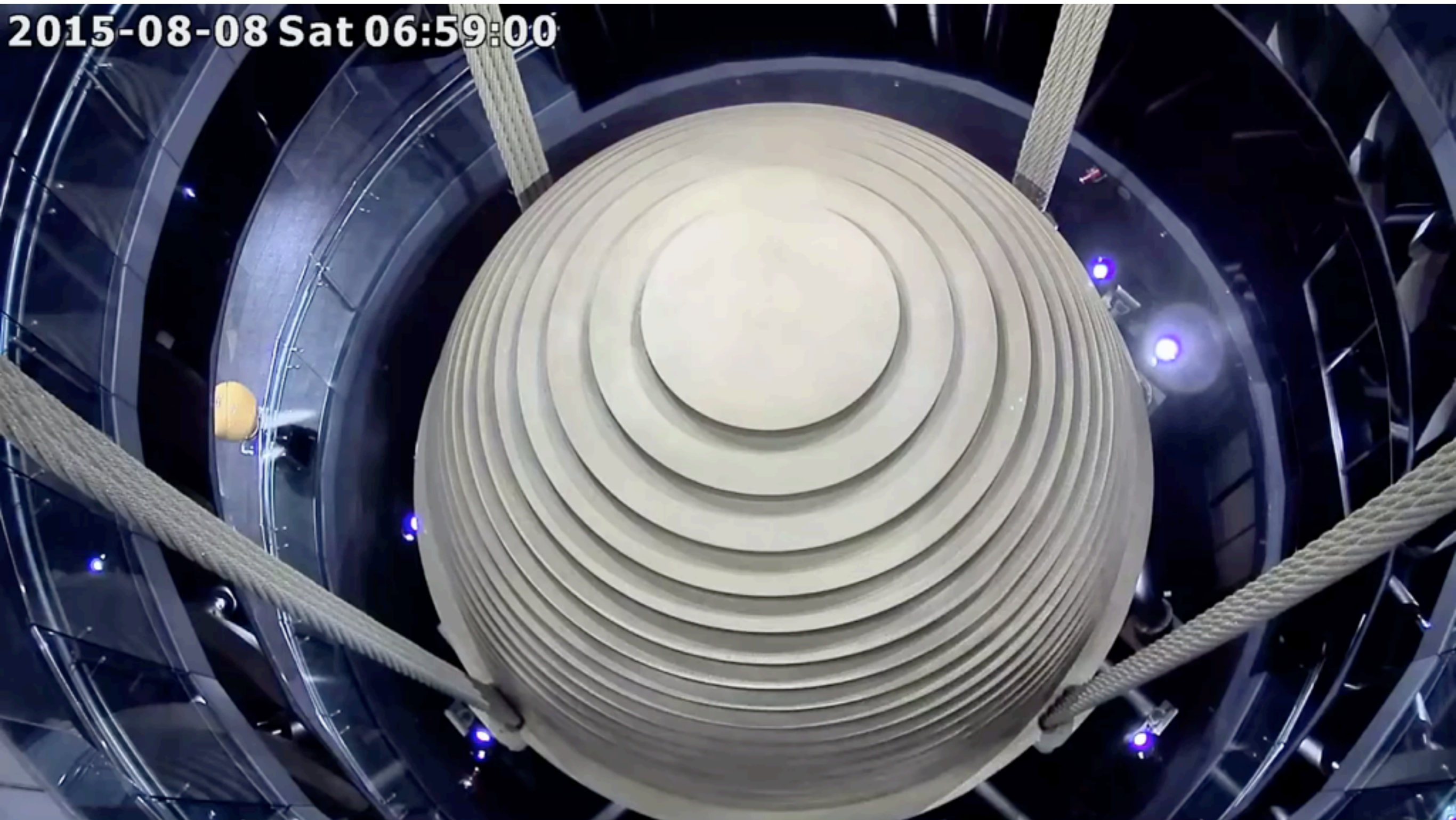


18.031

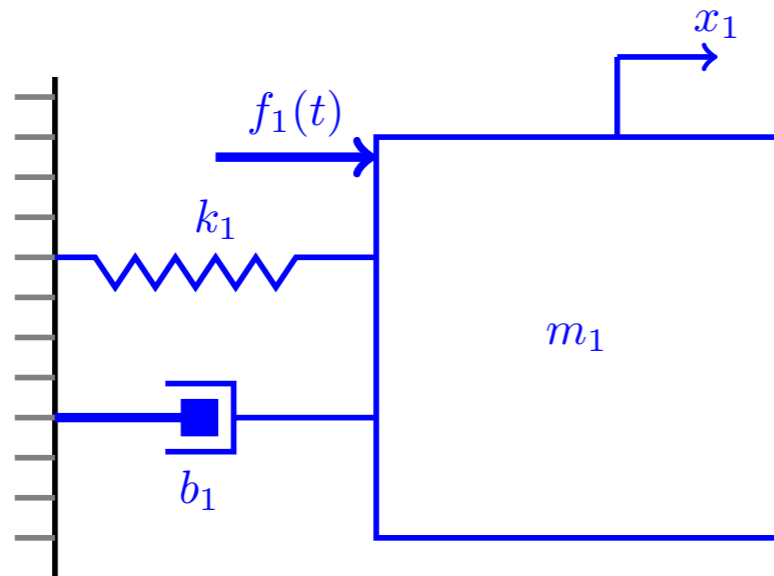
Day 8

Tuned mass damper



<https://www.youtube.com/watch?v=xqELmBNyWfU>

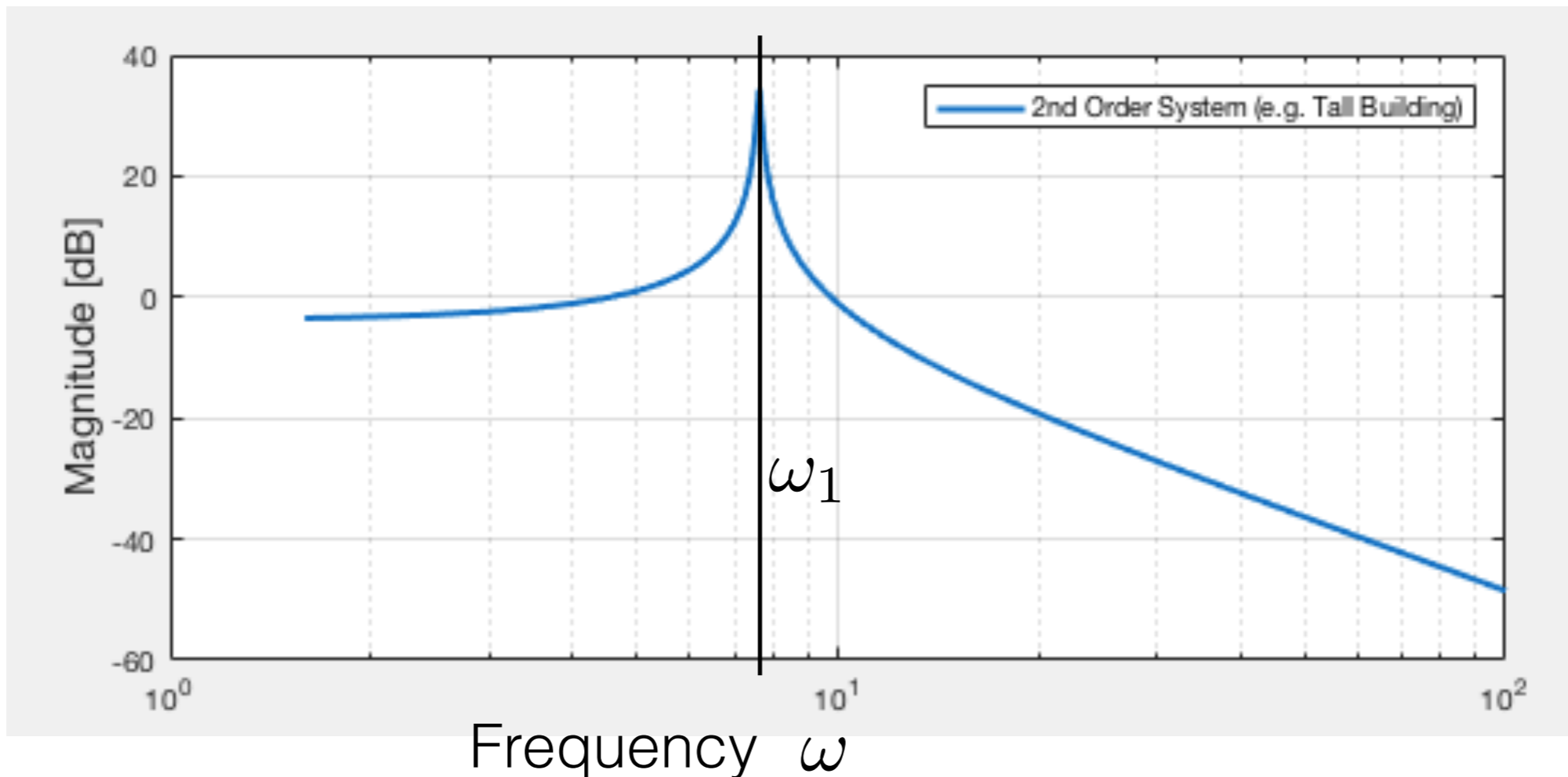
Mass 1 alone



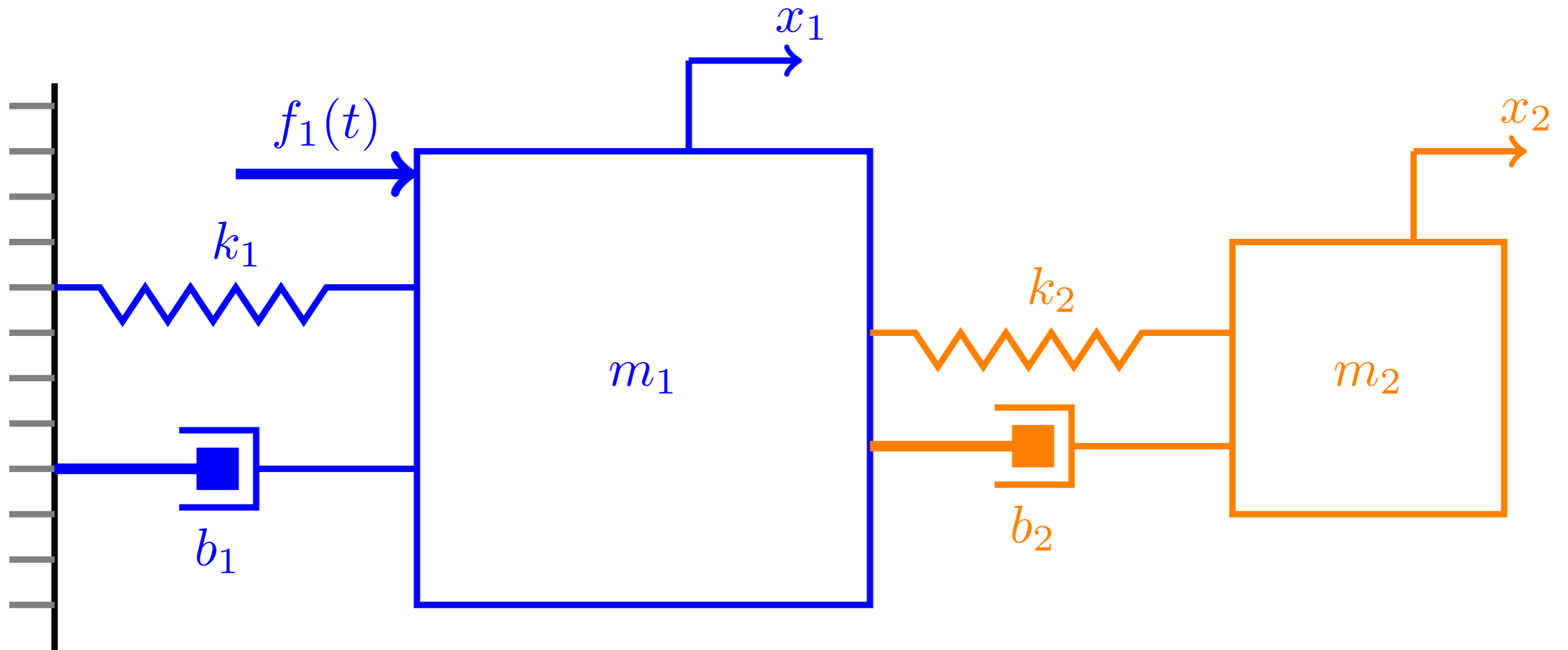
$$m\ddot{x}_1 + b_1\dot{x}_1 + k_1x_1 = f_1(t)$$

$$H(s) = \frac{1}{ms^2 + b_1s + k_1}$$

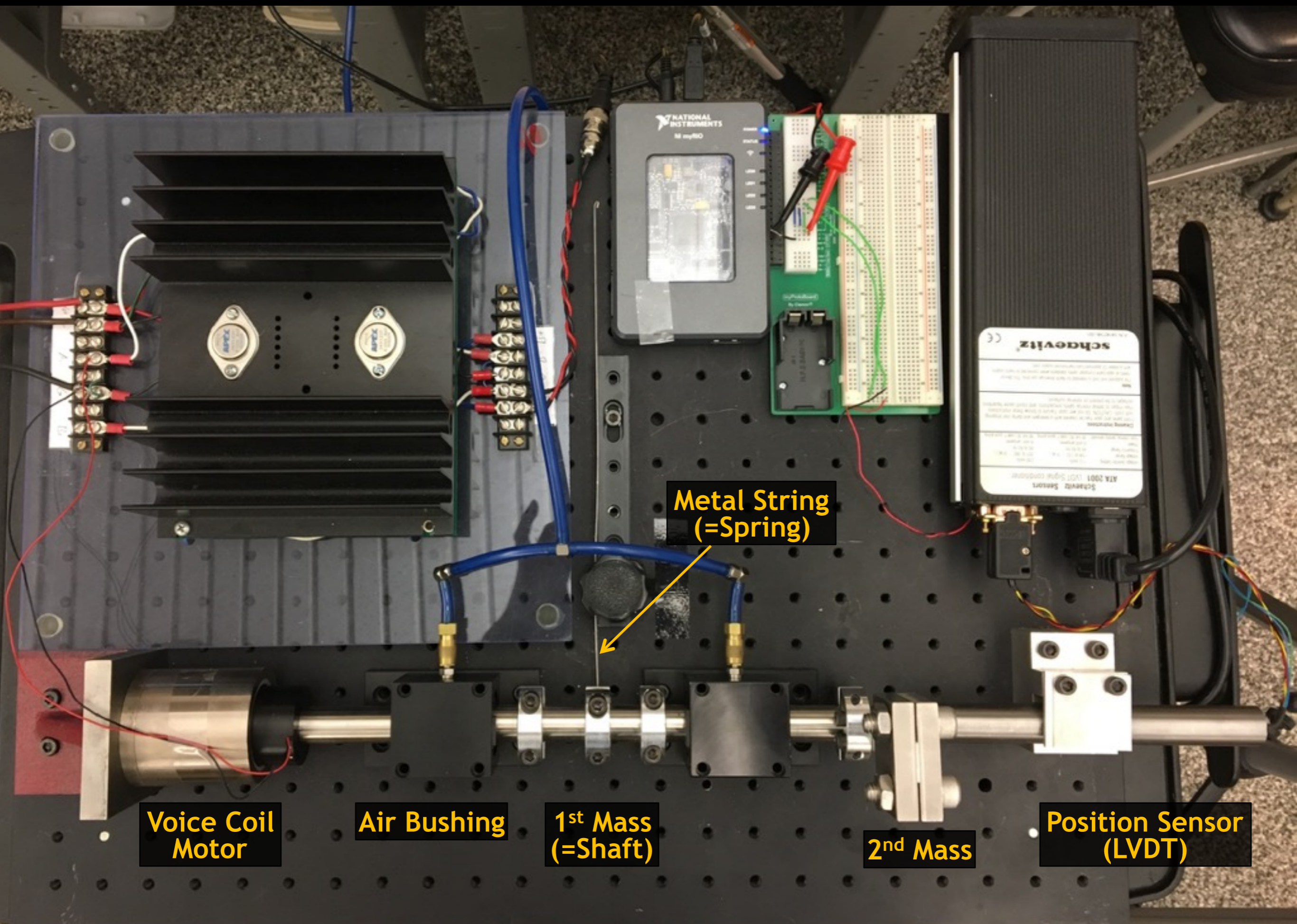
$|H(i\omega)|$
(gain)



Tuned mass damper



effective way to remove resonance of first mass m_1



Voice Coil Motor

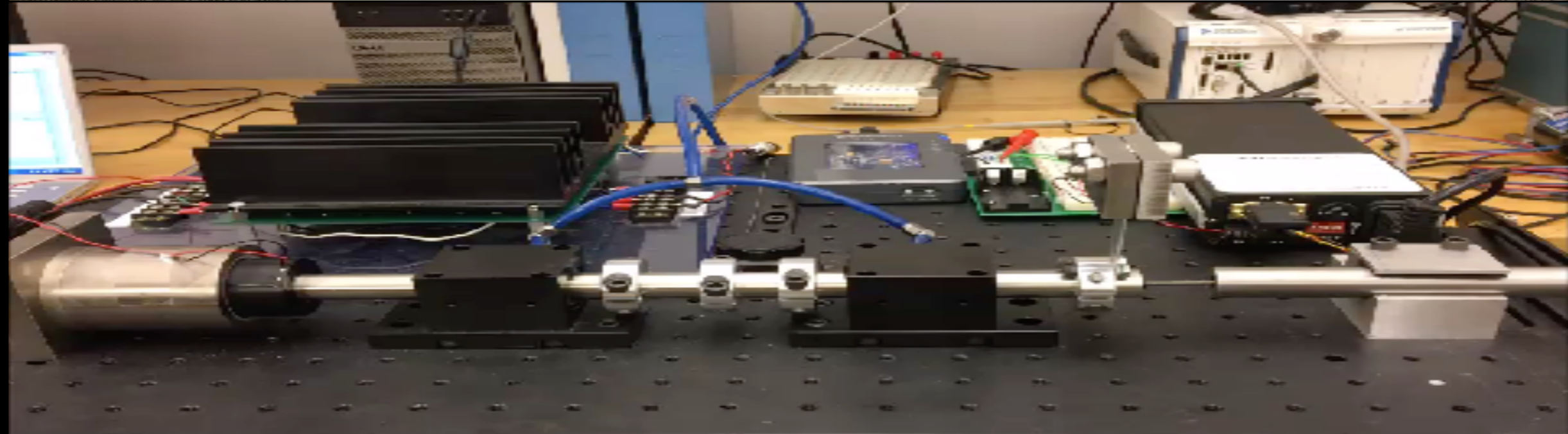
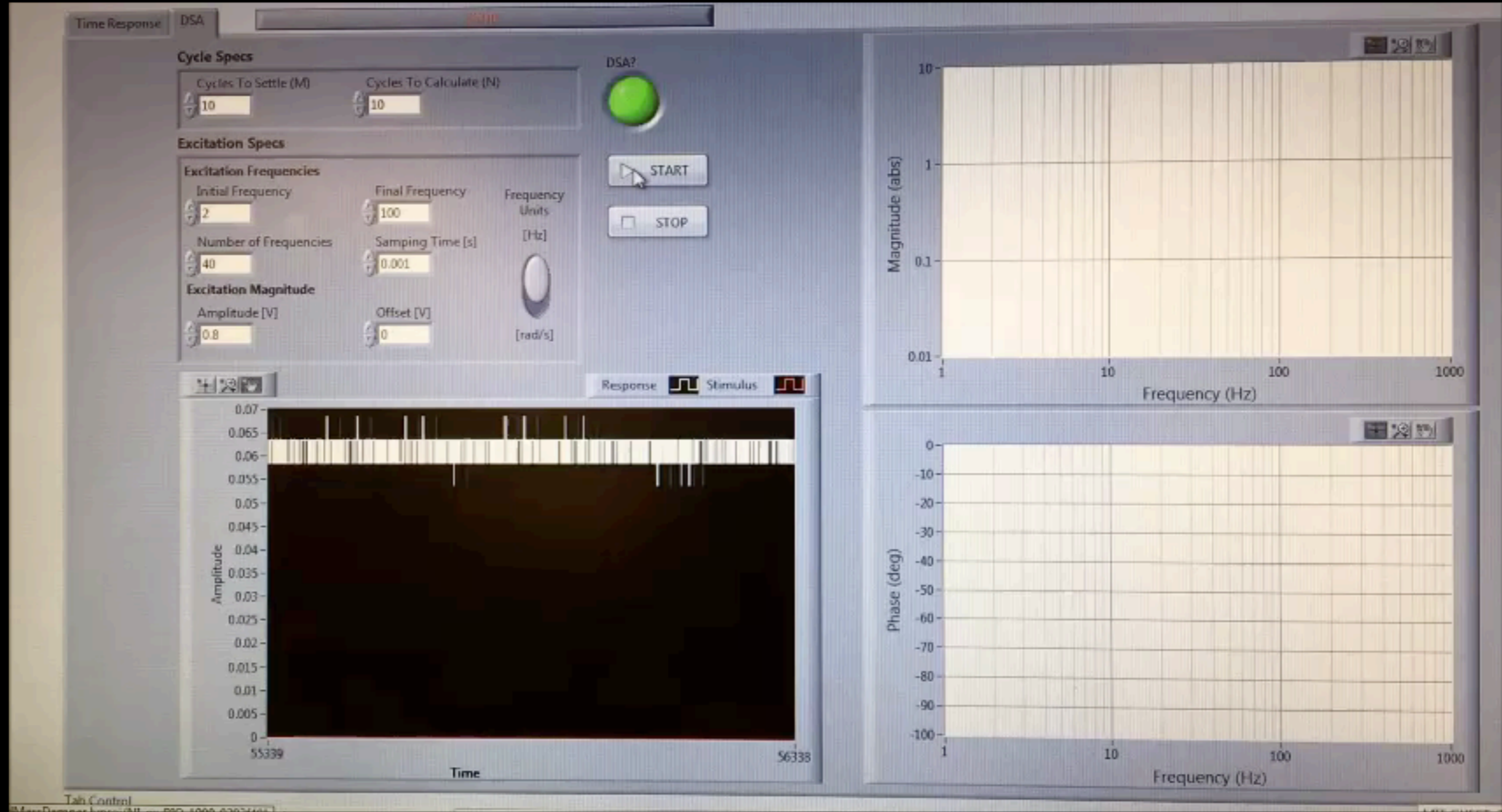
Air Bushing

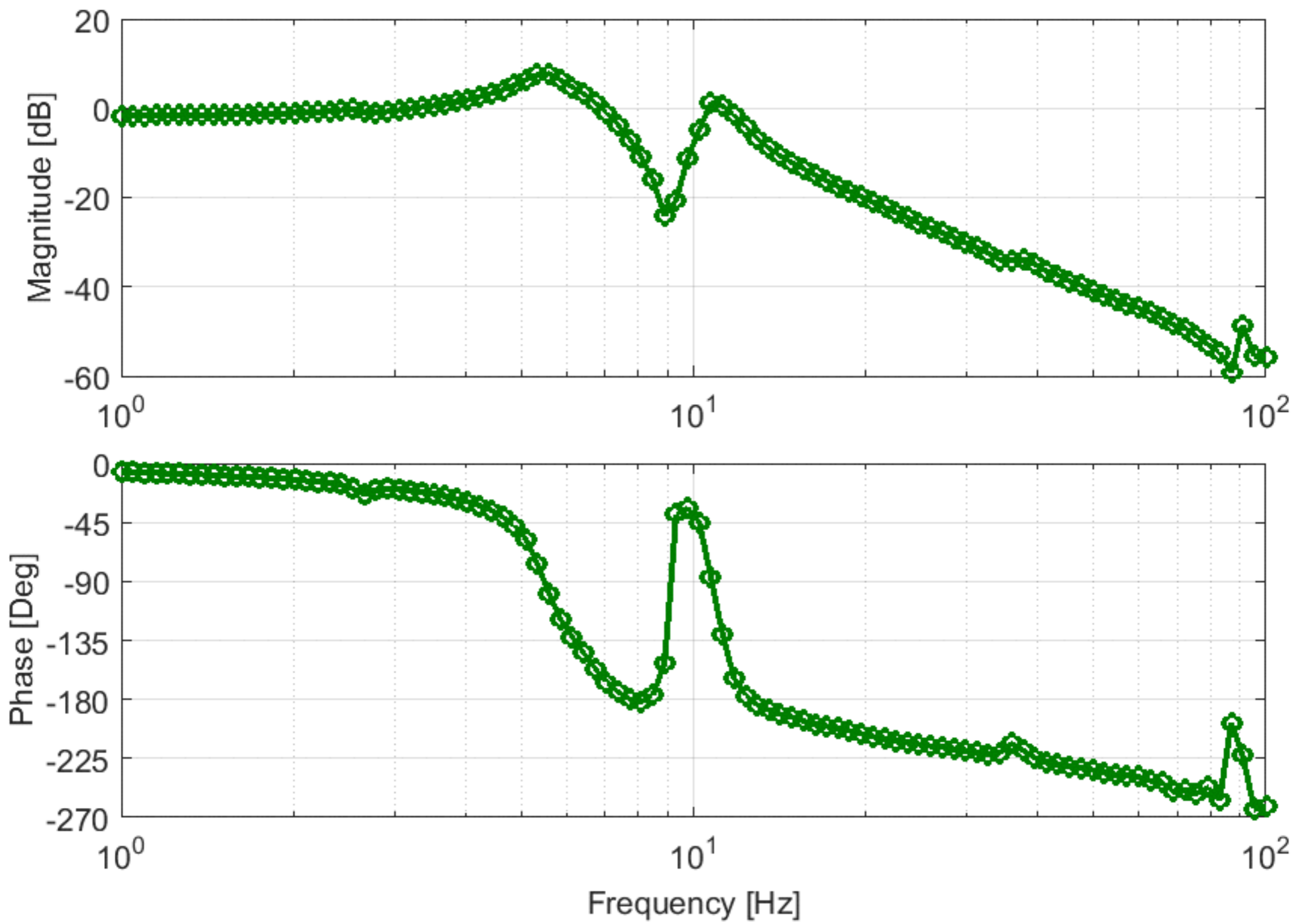
1st Mass (=Shaft)

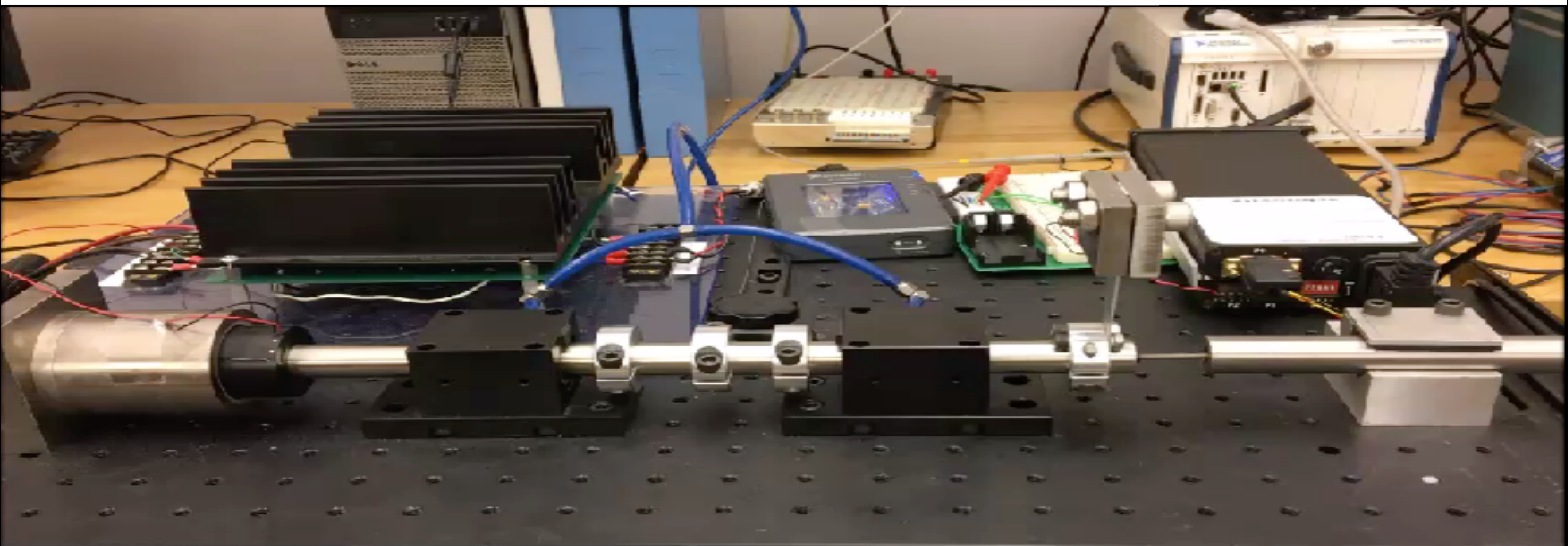
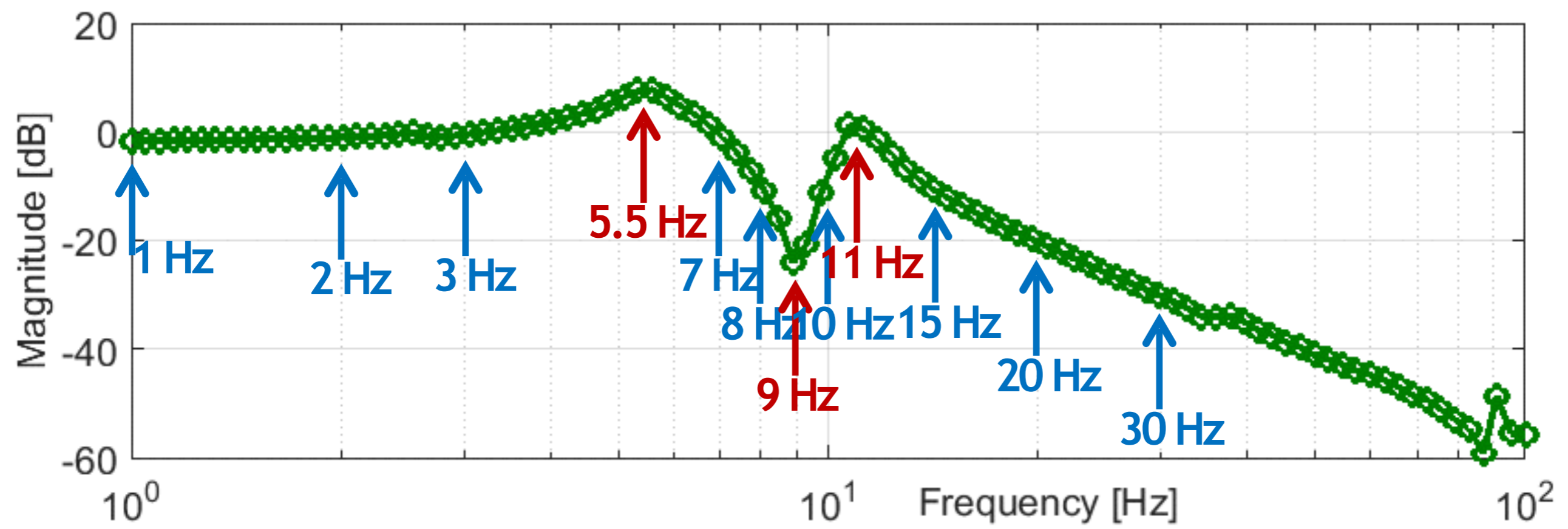
2nd Mass

Position Sensor (LVDT)

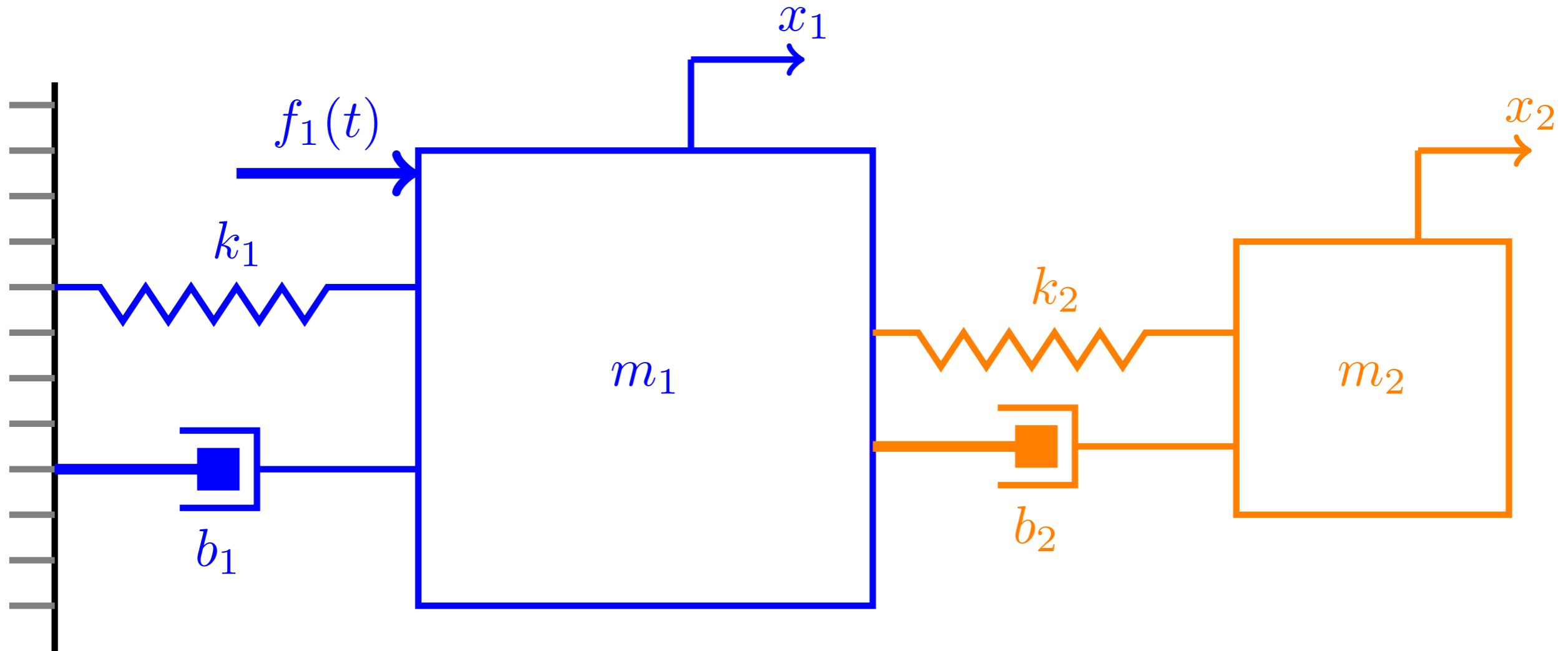
Metal String (=Spring)







Tuned mass damper



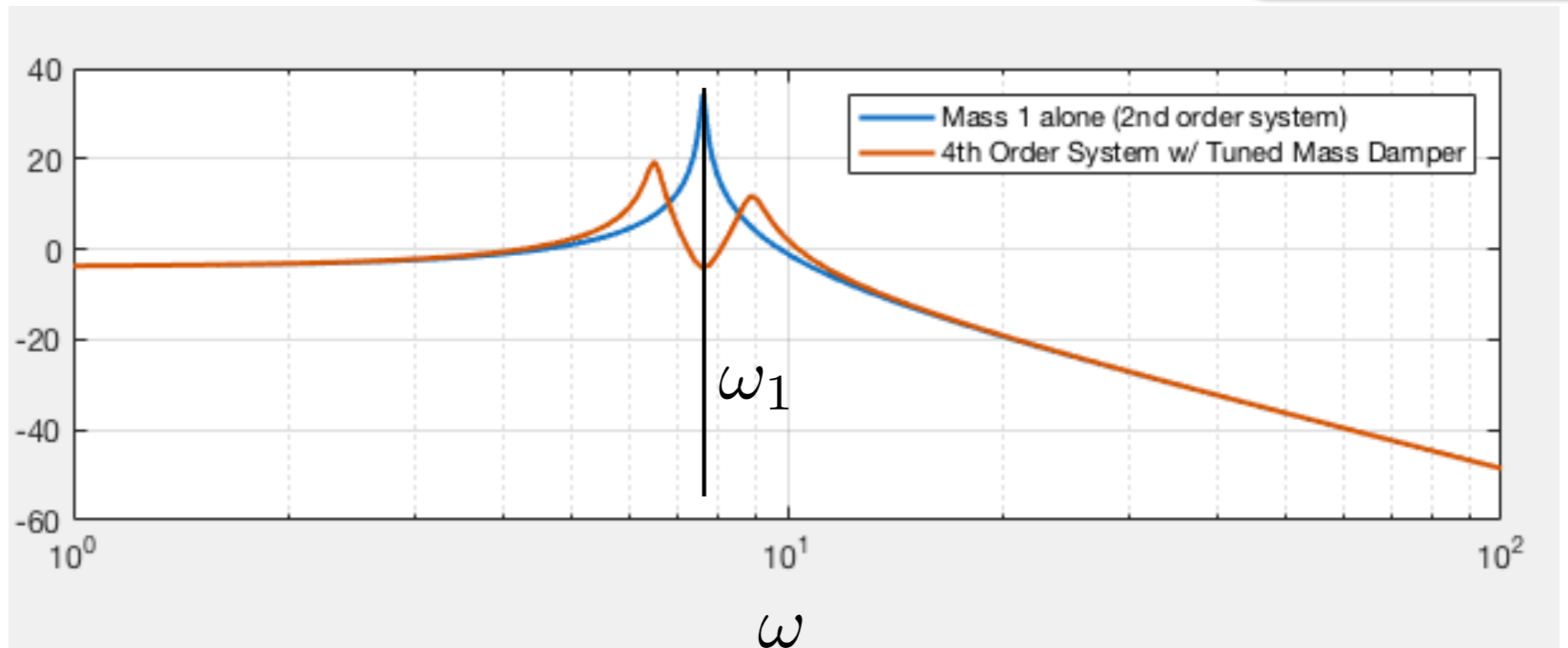
Mechanical parameters:

$$\begin{array}{lll} m_1 = 0.85 & b_1 = 14 & k_1 = 1950 \\ m_2 = 0.3 & b_2 = 0.4 & k_2 = 947.5 \end{array}$$

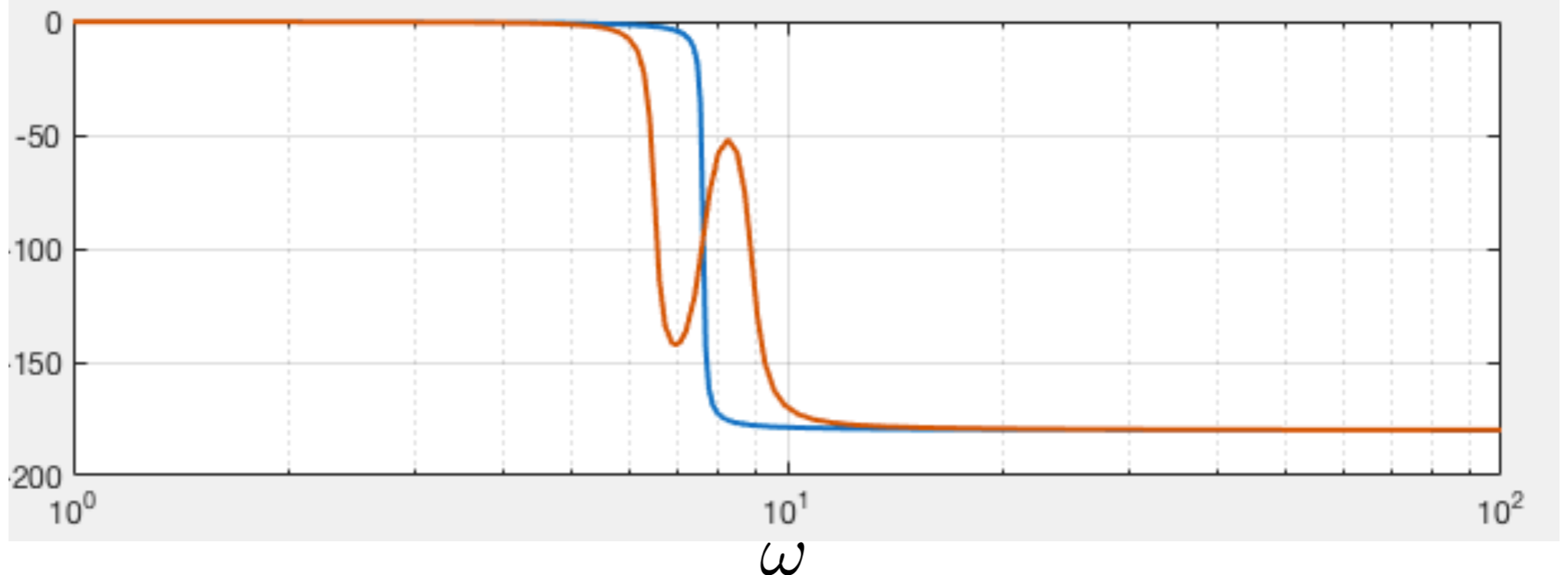
System function for x1

$$X_1 = \frac{P_2}{P_1 P_2 + m_2 s^2 Q_2} F_1 = H(s)$$

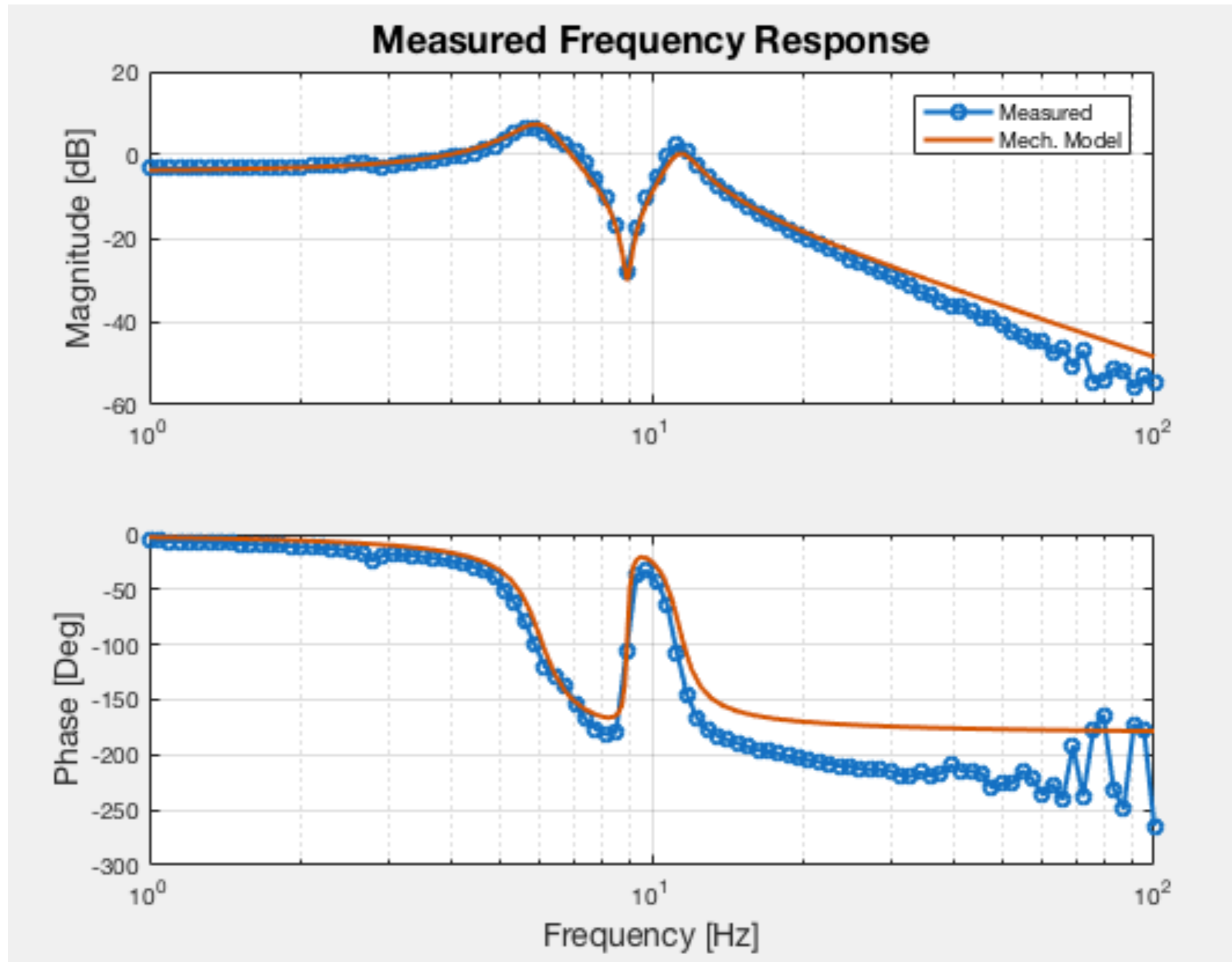
$|H(i\omega)|$
(gain, dB)



$-\phi(i\omega)$
(phase gain)

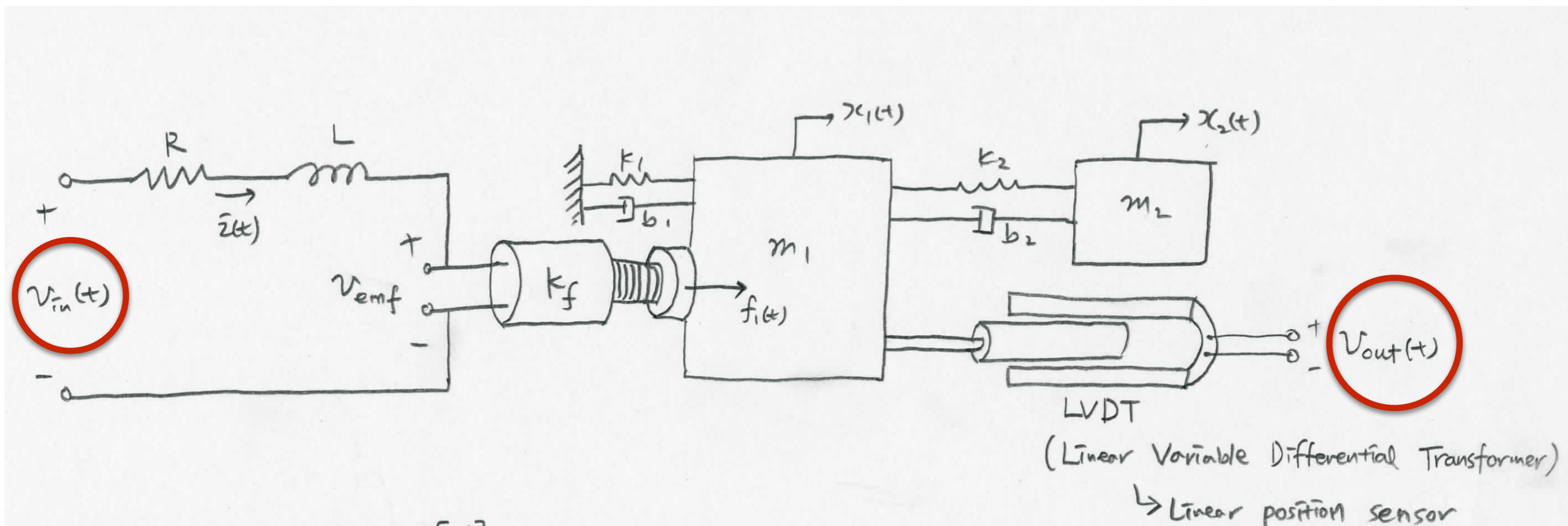


Comparing with experimental data



Improving the model

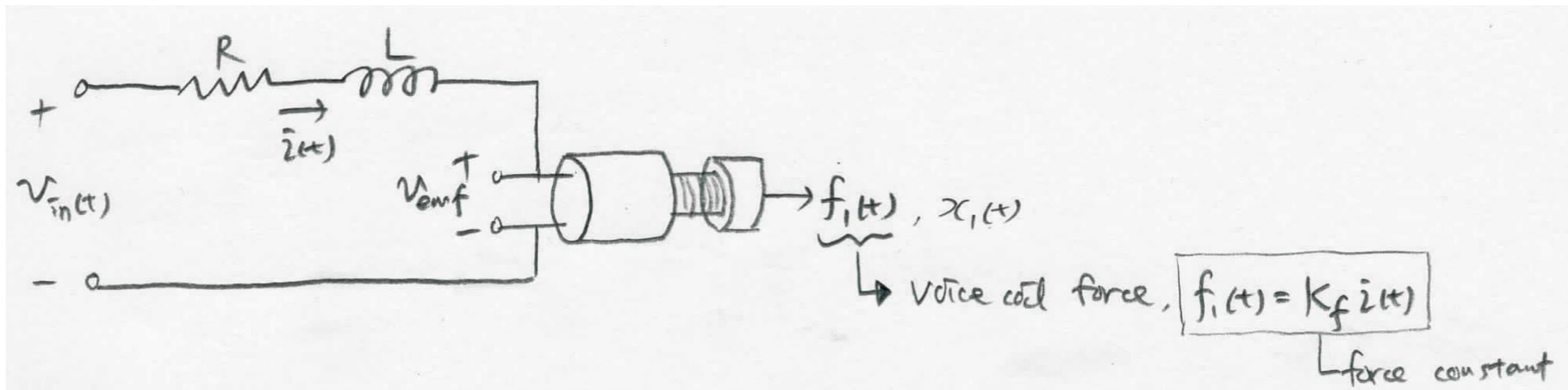
- Take electric circuit driving the system into account:



Experiment: Input is $V_{in}(t)$, measured output is $V_{out}(t)$

External forcing f_1 itself is the response of an electric system!

Electric system



- $v_{in}(t)$ = input voltage [V]
- v_{emf} = Back EMF (Electro-Motive Force) [V]
- R = resistance of voice coil actuator system [Ω]
- L = inductance " [H]
- K_f = force constant [N/A]

What is system function from $V_{in}(t)$ to $f_1(t)$?

Electric system

Electrical
parameters

$$\alpha = 1250$$

$$R = 1$$

$$L = 5 \cdot 10^{-3}$$

$$k_f = 1$$

