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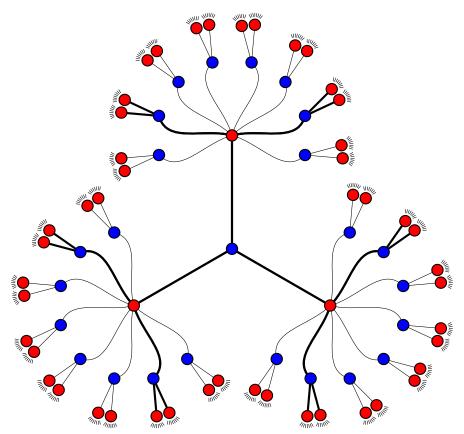


Figure 1. Building of U(2) inside U(3) (unramified)

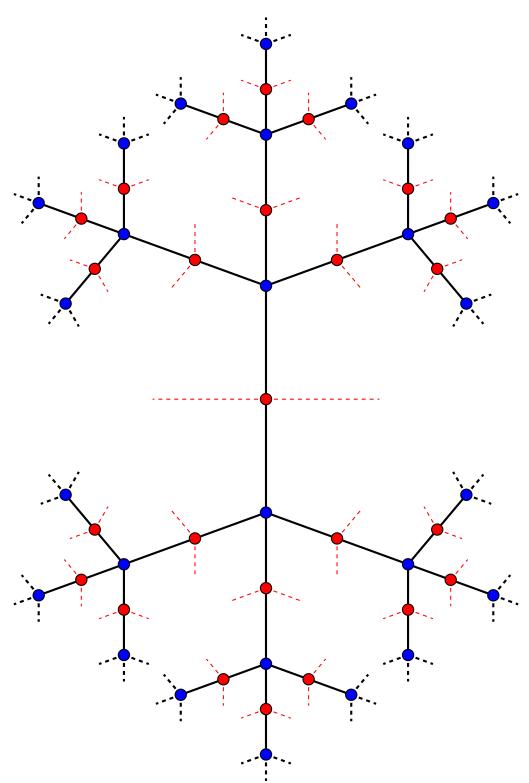


Figure 2. Building of U(2) inside U(3) (ramified)

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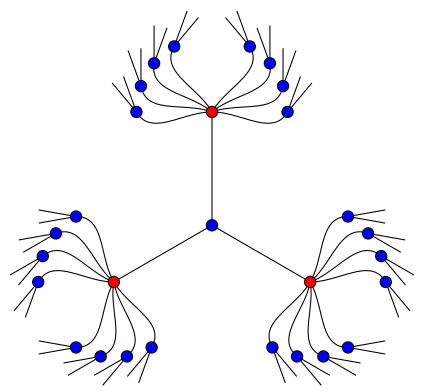


Figure 3. Building of unramified U(3) over  $\mathbb{Q}_2$ 

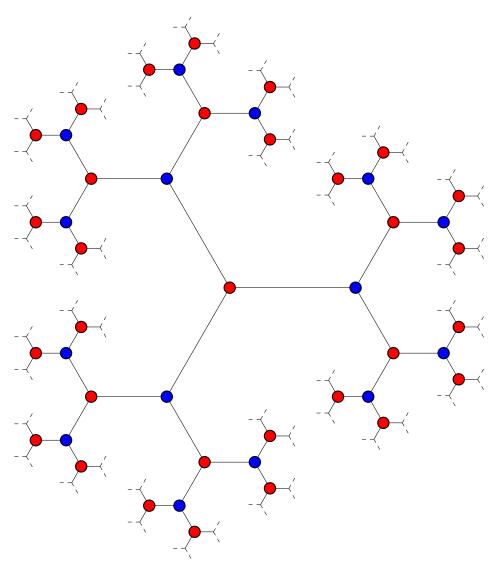


Figure 4. Building of  $\mathrm{SL}_2(\mathbb{Q}_2)$  with coloring

Figure 5. Building of type  $A_2$  over  $\mathbb{Q}_2$  with the fundamental apartment in red

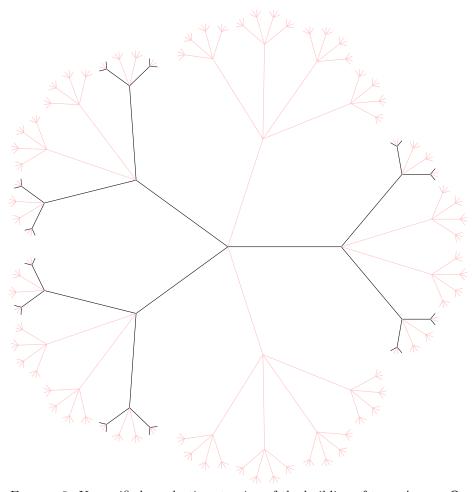


Figure 6. Unramified quadratic extension of the building of type  $A_2$  over  $\mathbb{Q}_2$ 

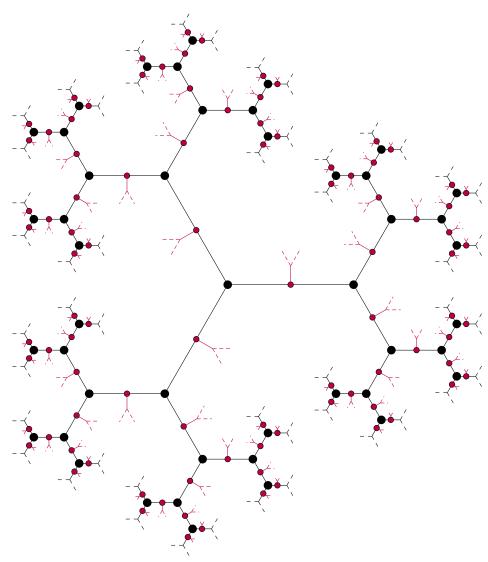


Figure 7. Ramified quadratic extension of the building of type  $A_2$  over  $\mathbb{Q}_2$ 

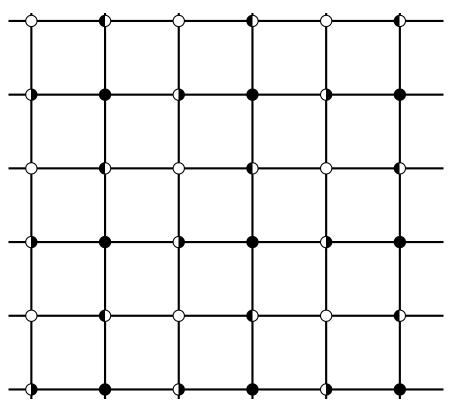


Figure 8. Apartment of the building of  $\mathrm{SL}_2 \times \mathrm{SL}_2$  with coloring

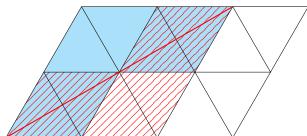


FIGURE 9. Two minimal galleries and the unique geodesic between points. We see that chambers traversed by the geodesic are in the minimal gallery.

Starting at the first chamber, we always make sure we go to a chamber where the normal vector of wall between chambers is in the closest to direction of the geodesic.

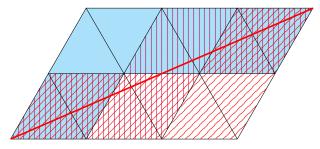


FIGURE 10. Three minimal galleries and the unique geodesic between points.

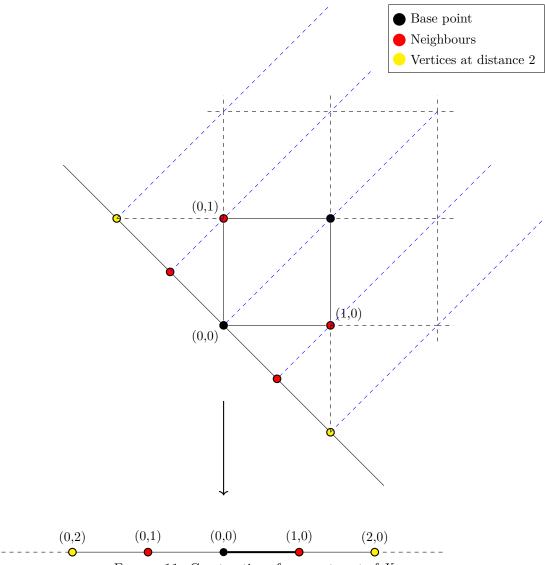


Figure 11. Construction of an apartment of  $X_{\mathrm{GL}_2}$ .

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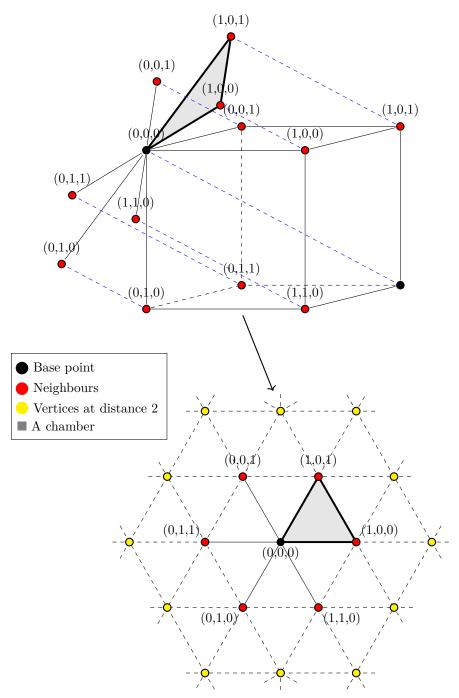


Figure 12. Construction of an apartment of  $X_{\mathrm{GL}_3}$ .

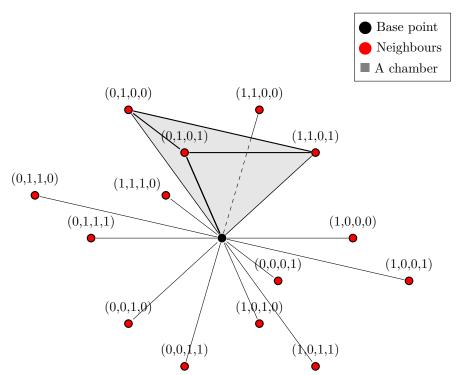


FIGURE 13. Neighbours of a point within an apartment of  $X_{\mathrm{GL}_4}$ .

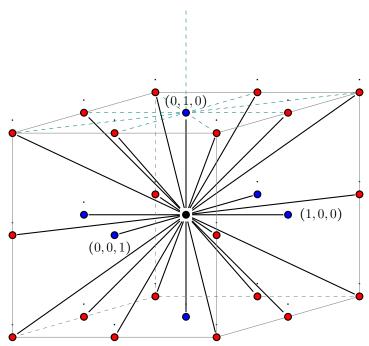


FIGURE 14. Neighbours of  $x_0$  in the fundamental apartment of  $X_{\mathrm{GSp}_6}$ .

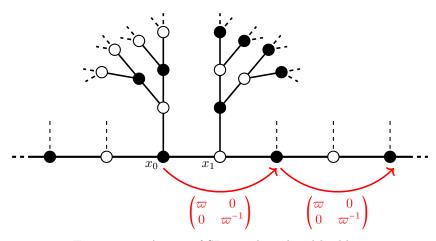


Figure 15. Action of  $\mathrm{SL}_2$  on the colored building

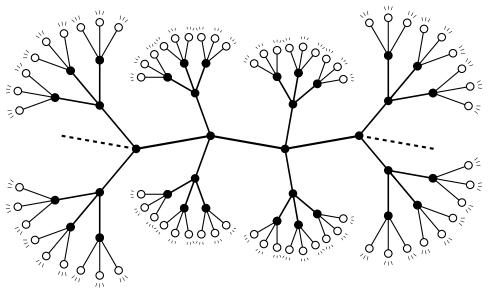


FIGURE 16. Tube of radius 2 around an apartment: vertices fixed by  $\begin{pmatrix} a & 0 \\ 0 & b \end{pmatrix}$  with  $\nu(1-a/b)=2$ .

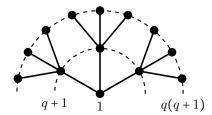


Figure 17. Vertices in a ball of radius 2 centered at a vertex, with q=2

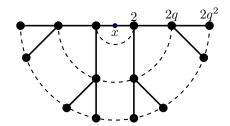
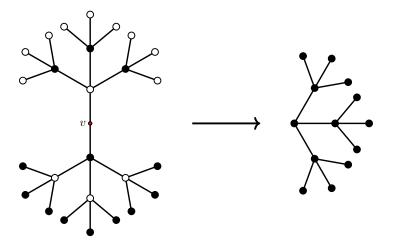


Figure 18. Vertices in a ball of radius 2 centered at a midpoint, with q=2



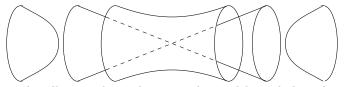


FIGURE 19. An elliptic orbit, nilpotent orbit and hyperbolic orbit in  $\mathfrak{sl}_2(\mathbb{R})$  (in order of appearance from left to right)

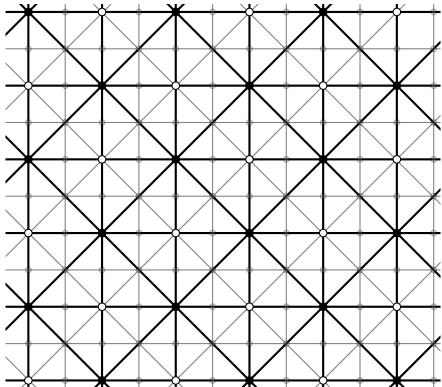


FIGURE 20. Apartment of the building of type  $C_2$  after a ramified extension. Note that the white vertices are not hyperspecial in the base building (they have only 4 neighbors) become hyperspecial after the extension

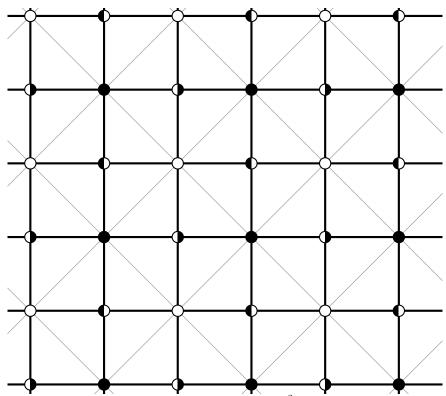


FIGURE 21. Apartment of the building of type  $A_2^2$  inside the building of type  $C_2$ . The group  $SL_2 \times SL_2$  preserves all 4 patterns, and  $GSp_4$  preserves the 2 types of patterns (monochrome to monochrome, bichrome to bichrome)

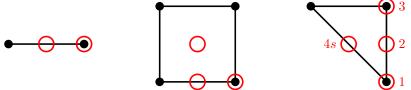


Figure 22. Possible parahorics corresponding to elliptic elements in  $GL_2$ ,  $GL_2 \times GL_2$  and  $GSp_4$  from left to right.

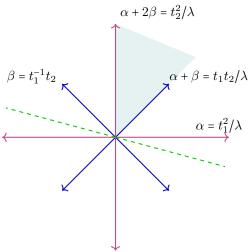


FIGURE 23. Root system of  $\mathrm{GSp}_4$  with choice of positive roots, the long roots is the root system of H. Shaded is the positive Weyl Chamber of G.

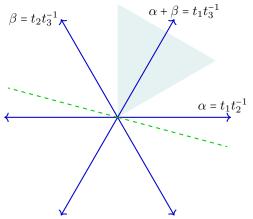


FIGURE 24. Root system of type  $A_2$ 

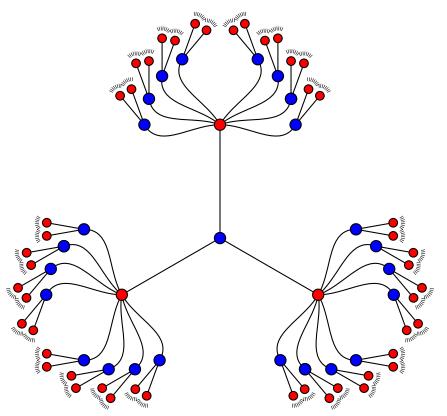


Figure 25. Building of unramified U(3) v.2

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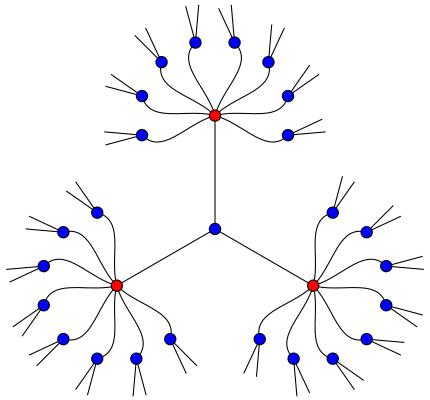
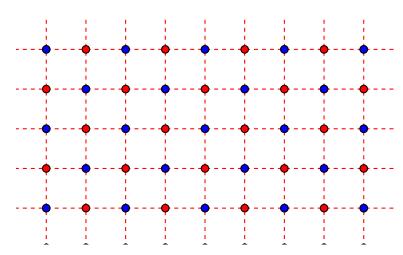
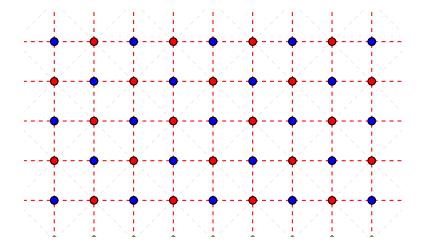


Figure 26. building of unramified U(3) v.3

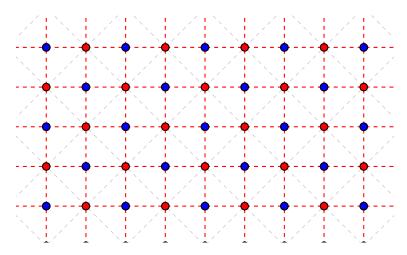
Apartment in the building of type  $A_2^2$  (SL<sub>2</sub>):



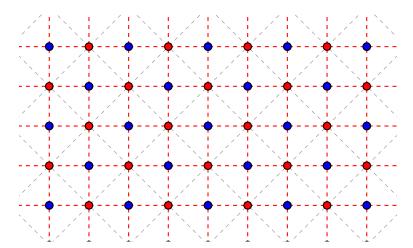
Apartment in the building of type  $\mathcal{A}_2$  (S§2):



Apartment in the building of type  $\mathcal{Q}_2$  ( $\mathrm{Sp}_{2}^2$ ):



Apartment in the building of type  $C_2$  (Sp<sub>4</sub>):



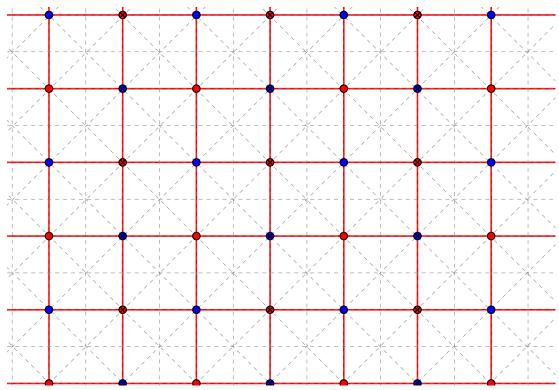


FIGURE 27. Apartment of the building of type  $A_2^2$  inside the building of type  $C_2$ .

 $\mathrm{GL}_2^2$  acts transitively on vertices,  $(\mathrm{GL}_2^2)^0$  preserves colors, and  $\mathrm{SL}_2^2$  preserves colors and patterns.