

All questions except number 1,5 come from the course text.

1. This question consist on a few short multiple choice questions on precalc to discuss.

(a) Given the equation of a line  $y = mx + b$ ,  $m$  is called the:

asymptote    slope    multiplier     $x$ -intercept     $y$ -intercept

(b) The lines  $y = m_1x + b_1$  and  $y = m_2x + b_2$  are *parallel* if:

$m_1 = m_2$      $m_1m_2 = -1$      $m_1m_2 = 1$      $b_1 = -b_2$      $m_1b_2 - b_1m_2 = 0$

What about *perpendicular*?

(c) The maximum of  $-2x^2 + 12x + 10$  is attained for:

- $x = 3$   
  $x = 3 \pm \sqrt{14}$   
  $x = 0$   
  $x = 28$   
  $x$  in the middle of the two  $x$ -intercepts

Can you recall how to determine if quadratic has a maximum/minimum? What's the quadratic formula?

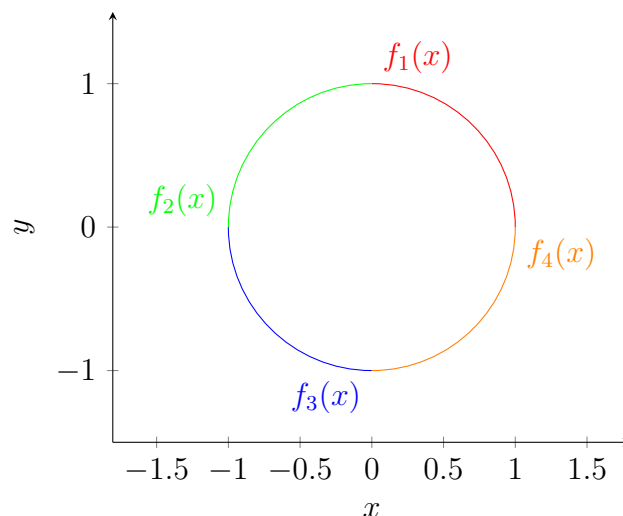
(d) Which of the following assertion is true?

$\ln(x + y) = \ln(x) + \ln(y)$      $e^{xy} = e^x e^y$      $2^x + 2^x = 2^{x+1}$      $f^{-1}(x) = \frac{1}{f(x)}$

2. Let  $f(x) = \sqrt{x+2}$  for  $x \geq -2$ . Find the inverse of  $f(x)$  for  $x \geq -2$  and write it in the form  $y = f^{-1}(x)$ . Then, verify the relationships  $f(f^{-1}(x)) = x$  and  $f^{-1}(f(x)) = x$ .

3. The unit circle  $x^2 + y^2 = 1$  consists of four one-to-one functions,  $f_1(x)$ ,  $f_2(x)$ ,  $f_3(x)$ , and  $f_4(x)$  (see figure).

- Find the domain and a formula for each function.
- Find the inverse of each function and write it as  $y = f^{-1}(x)$ .



4. Solve the following equations:

- $\log_{10} x = 3$ .
- $\log_8 x = \frac{1}{3}$ .

•  $\ln x = -1$ .

5. Without using a graphing utility, sketch the graph of  $y = 2^x$ . Then on the same set of axes, sketch the graphs of  $y = 2^{-x}$ ,  $y = 2^{x-1}$ ,  $y = 2^x + 1$ , and  $y = 2^{2x}$ .
6. (\*) A particular factory produces organic, artisanal garbage; denote by  $x$  the number of units of garbage the factory produces in a given day.
1. Suppose the total cost to the factory of producing  $x$  units a day is  $C(x) = 36x + 260$  dollars, and that the total projected revenue from producing  $x$  units a day is  $R(x) = -2x^2 + 104x - 220$ . Find the projected daily profit from producing  $x$  units per day.
  2. Determine the number of units of artisanal garbage the factory should produce each day to maximize its profit.
7. (\*) Prove that, if  $b > 0$ ,  $c > 0$ ,  $b \neq 1$ ,  $c \neq 1$ , then  $(\log_b c)(\log_c b) = 1$ .
8. Sketch a function that is one-to-one and positive for  $x \geq 0$ . Make a rough sketch of its inverse.
9. Solve the equation  $3^{3x-4} = 15$