

Erratum to “A symmetric function generalization
of the chromatic polynomial of a graph”
[Adv. Math. 111 (1995) 166–194]

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Theorem 3.4 is incorrect as stated because the definition of a *maximal* partition on p. 179 is misstated. The correct definition is that a partition $\mu \vdash r \leq d$ with exactly l nonzero parts is *maximal* if μ is allowable and for every other allowable partition ν of an integer $s \leq d$ (where s need not be equal to r), either $\nu_i = \mu_i$ for all $1 \leq i \leq l$, or there exists $i \leq l$ such that $\nu_1 + \cdots + \nu_i < \mu_1 + \cdots + \mu_i$. With this corrected definition, Theorem 3.4 and its corollaries are correct as stated.

The proof of Theorem 3.4 is essentially correct once the definition of “maximal” is corrected, but a few minor corrections need to be made. The definition of φ_μ at the bottom of p. 179 should read

$$\varphi_\mu(Q_S) = \begin{cases} 1, & \text{if } r = d \text{ and } S = \{\mu_1, \mu_1 + \mu_2, \dots, \mu_1 + \cdots + \mu_{l-1}\}, \\ t, & \text{if } r = d - 1 \text{ and } S = \{\mu_1, \mu_1 + \mu_2, \dots, \mu_1 + \cdots + \mu_l\}, \\ t(t-1)^i, & \text{if } r \leq d - 2 \text{ and } S = \{\mu_1, \mu_1 + \mu_2, \dots, \mu_1 + \cdots + \mu_l, \\ & \mu_1 + \cdots + \mu_l + i + 1, \mu_1 + \cdots + \mu_l + i + 2, \dots, d - 1\}, \\ 0, & \text{otherwise,} \end{cases}$$

and corresponding straightforward adjustments to the *Proof of Claim* on p. 180 should be made. Finally, on the third line from the bottom of p. 180, “ $a_\lambda \neq 0$ ” should be changed to “ $a_\nu \neq 0$ for some $\nu \geq \lambda$ ”, and “ P_λ ” in the displayed equation at the top of p. 181 should be changed to “ X_{P_λ} ”.

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