ERRATA

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- page 8, Exercise 5, line 3. Change G to H_n.
- page 9, Exercise 13. It should be assumed that G is a simple graph. (Otherwise one has to consider "adjacency with multiplicity").
- page 13, line 4. Change the first $=$ to $\neq$.
- page 14, first line after (2.4). Change "(u, v)-entry of the matrix Φ_Δ" to "(u, v)-entry (short for (f_u, f_v)-entry) of the matrix $[\Phi_\Delta]$".
- page 16, line 5. Change $(-1)^{u+w}$ to $(-1)^{u \cdot w}$.
- page 18, Exercise 2(a). Assume that $k \leq n/2$.
- page 22, line 11–. It actually was not previously assumed (though it should have been) that "G is connected and has at least two vertices." Moreover, connected graphs are not defined until page 135.
- page 23, line 2–. $\mu(w, v)$ is the same as μ_{wv} (the number of edges between u and v). Also on page 24, equation (3.5) and line 8–.
- page 25, line 2. Change the last $\boldsymbol{B}^{m-1}$ to $\boldsymbol{B}^{m+1}$.
- page 26, line 3. The claim that $0 \leq \sigma_i \leq 1$ is not true. We need to work with the row sums, not the column sums. Essentially, the argument works with $\boldsymbol{N_i}$ replaced by the transpose $\boldsymbol{N_i}^t$.
- page 26, line 4. Change $V\boldsymbol{N_i}U$ to $V\boldsymbol{N_i}^tU$.
- page 29, Exercise 8, line 2. Change n^2 to $(n-1)^2$.
- page 29, line 3–. Change $H(u, v)$ to $H_k(u, v)$.
- page 32, line 3–. Change "We call P_i the ith *level*" to "We call P_j the jth *level*". (While this does not affect the meaning, it's obviously better to keep the notation consistent.)
- page 71, line 11–. Change "Exercise 5" to "Exercise 6.5".

- page 83, line 7. Add "or *cycle enumerator*" after "*cycle index polynomial*" (since the term "cycle enumerator" is used later in the text).
- page 87, line 10–. Change "is a line" to "in a line".
- page 93, line 14–. Change $\frac{1}{4}$ to $\frac{1}{8}$.
- page 94, line of table beginning $2, 1, 1$. Change $(12, 23)$ to $(13, 23)$.
- page 95, line 4. Change $\sum_{i=0}^{i(i-1)}$ to $\sum_{i=0}^{12}$.
- page 109, line 10–. Change $n - i + 1$ to $i - n - 1$.
- page 110, line 6. Change "from $\emptyset$ to w" to "from $\emptyset$ to λ".
- page 116, line 14–. Change $\sum_{m_k \geq 1}$ to $\sum_{m_k \geq 0}$.
- page 116, line 2–. Change "most r" to "most s".
- page 127, Exercise 14, line 4. Change I to I.
- page 129, line 3–. Although the meaning is clear, for consistency of notation one should change 1 to I.
- page 140, line 9–. Change f_j to f_i.
- page 142, line 7–. Change $p \cdot \det(\boldsymbol{L_0})$ to $-p \cdot \det(\boldsymbol{L_0})$.
- page 144, lines 9 and 10. Change T_2 to T_1 (twice).
- page 145, line 5–. Change "rooted" to "planted".
- page 146, figure at top of page. The figure is missing six planted forests at the top level, viz., the six planted forests with one endpoint. There are $3!t(3) = 18$ maximal chains in all.
- page 146, line 10. Change "one" to "zero".
- page 151, line 14–. Insert before the period at the end of the sentence: ", denoted $\mathrm{init}(e)$ and $\mathrm{fin}(e)$, respectively".
- page 151, line 13–. Change "Definition 8.5" to "Definition 9.5".

- page 151, Theorem 10.1. The definition of a connected digraph needs to appear before this theorem. First one should define a *walk* in a digraph in an obvious way analogous to the undirected case. A digraph D is *strongly connected* if it is nonempty and there is a walk from any vertex u to any vertex v. A digraph D is *weakly connected* if it is connected as an undirected graph, i.e., after replacing each directed edge, say from u to v, with an undirected edge incident to u and v. Theorem 10.1 is true with either definition of connectedness.

- page 152, line 11–. Change "unique directed path" to "unique directed walk". (Otherwise the digraph with vertices $1, 2, 3$, where $v = 3$, and edges $1 \to 2, 2 \to 1, 2 \to 3$ is an unwanted example.)

- page 152, line 9–. Insert after "$1 \leq i \leq r - 1$." the parenthetical sentence "(All three of these conditions are considered to be vacuously true if the sequence $e_1, \ldots, e_r$ is empty.)"

- page 152, line 7–. Insert before "There is ..." the sentence "From now on, an oriented subtree of D will always mean a subdigraph of D that is an oriented tree with the full vertex set V, or in other words, a *spanning* oriented subtree of D."

- page 153, line 2. While this line is correct as it stands, it would be logically better to replace "$\mathrm{init}(e(u)) = u$" with "$\mathrm{init}(e_j) = u$".

- Proof of Theorem 10.4. The induction is not quite correct since in the statement of the theorem it is assumed that D is connected, while D_1 and/or D_2 may not be connected. This problem is easily fixed since the determinant of the reduced Laplacian matrix $\boldsymbol{L}_0(D)$ of a disconnected digraph D is clearly 0 [why?], and the number of oriented spanning subtrees (with any root) of a disconnected graph is also clearly 0.

- page 156, Example 10.8, line 3. Change a_{2^m} to a_{2^n}.

- page 156, lines 3– to 1–. The definition of D_n is not quite right when $n = 1$, where we need two edges rather than one. It would be better to say that the edges of D_n are binary sequences $a_1 \cdots a_n$ with initial vertex $a_1 \cdots a_{n-1}$ and final vertex $a_2 \cdots a_n$.

- page 157, line 10–. Change $\boldsymbol{L}(D_n)$ to $\boldsymbol{L}_0(D_n)$.

- page 157, Lemma 10.9, line 2. Change "walk" to "path".
- page 158, line 5. To be precise, this definition does not work when $n = 1$.
- page 163, line 3–. Insert "to" before second "do".
- page 164, line 1. Change "Suppose that C" to "Suppose that a circuit C".
- page 171, line 11–. Change "real matrix" to "real".
- page 172, line 7. Change $\boldsymbol{C}^*_{T_1}$ to $\boldsymbol{C}_{T_1}$.
- page 174, line 1–. Change $\boldsymbol{C}_T$ to $\boldsymbol{B}_T$.
- page 183, diagram of squared square. There is an unlabelled 17×17 square.
- page 184, Exercise 5, line 2. Change "there in" to "there is".
- page 189, line 1. It should be stated before this sentence that the number of prisoners is $2n$.
- page 190, line 4–. Insert after "*Proof.*" the sentence "Take the vertex set of K_n to be $[n]$."
- page 190, line 2–. Change $1 \leq i \leq n$ to $1 \leq k \leq n$.
- page 191, line 4 above Section 2.4. Change X to S.
- page 194, line 16. Change "rows of $\boldsymbol{A}$" to "rows of $\boldsymbol{A} + I$".
- page 195, line 8–. Change $k \geq 2$ to $k \geq 3$.
- page 196, line 6–. insert after z^n the phrase "when n is odd".
- page 197, line 1–. It is assumed that $R \neq 0$ means $R \neq \{0\}$.
- page 199, first displayed equation. Change $\sum$ to $\prod$. ,
- page 201, line 5. Change "an" to "a".
- page 202, line 3. Remove the first].

- page 206, Exercise 25(b), line 2. Change $p_m(x)$ to $p_d(x)$.
- page 207, Exercise 28(c). It should be assumed that the rational function $F(x_1, \ldots, x_m)$ has a power series expansion $\sum_{i_1,\ldots,i_m \geq 0} c_{i_1,\ldots,i_m} x_1^{i_1} \cdots x_m^{i_m}$, that is, the formal product of the denominator of $F(x_1, \ldots, x_m)$ with the series equals the numerator of $F(x_1, \ldots, x_m)$.
- page 209, Hint 2.2. Change this hint to "Give an argument analogous to the proof of Theorem 8.9."
- page 211, Exercise 9.11, line 1. Change "numberof" to "number of".
- page 212, **12.26**. Insert "the equation" after "with respect to x".