Student Name (UNI): ____

Instructions:

This exam contains 5 pages (including this cover page) and 5 questions. The total number of possible points is **34 points**. You will have **65 minutes** to complete this exam.

- Print your name and UNI in the space above.
- Answer the questions in the space provided on the question sheets. Clear identify your answers.
- Write legibly and show your work, you may receive partial credit for intermediate steps. For questions requiring explanations, correct answers without any reasoning or work may not receive full credit.
- No calculators, computational devices, or consulting other people during the duration of this exam. Any cheating will result in an automatic failing grade in the course and potential administrative action.
- You may consult your notes and textbook for this exam.
- Upload your exam to Gradescope at the end of the time allotted.

Do not write in the table to the right.

Question	Points	Score
1	8	
2	12	
3	7	
4	4	
5	3	
Total:	34	

1. Consider the functions

$$f(x) = \begin{cases} \frac{1}{x} & \text{if } x \leq -1\\ x+1 & \text{if } x > -1 \end{cases}$$
$$g(x) = \cos(x)$$

(a) (2 points) State the domain and range of the function f(x).

(b) (3 points) Sketch the graph of the function f(x).

- (c) (3 points) Find the values: (i) f(-1)
 - (ii) f(0)
 - (iii) $(f \circ g)(0)$

2. Find the limit if it exists. If the limit does not exist, explain why.(a) (3 points)

$$\lim_{x \to \infty} \frac{x+1}{x}$$

(b) (3 points)

$$\lim_{x \to 1} \frac{x-1}{x^2-1}$$

(c) (3 points)

$$\lim_{x \to 2} 3^{\frac{1}{x-2}}$$

(d)	(3	points)
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 $\lim_{x \to -1} \frac{4x^2 + 7x}{x^3 + 1}$

3. Consider the function

$$f(x) = \begin{cases} x \sin\left(\frac{1}{x}\right) & x > 0\\ x & x \le 0 \end{cases}$$

(a) (3 points) Is f continuous at x = 0? Explain why or why not.

(b) (4 points) Show that f is or is not differentiable at x = 0 (and compute f'(0) if it is differentiable) using the definition of the derivative.

- 4. (4 points) Sketch the graph of an example of a function that satisfies all of the given conditions:
 - $\lim_{x \to -\infty} f(x) = -\infty$
 - $\lim_{x \to 0} f(x) = 0$
 - f(0) = 1
 - $\lim_{x\to 2^-} = \infty$
 - $\lim_{x\to 2^+} = 2$
 - $\lim_{x\to\infty} f(x) = 2$

5. (3 points) What does it mean for a function f(x) to be differentiable at a? To receive full credit, provide the definition using limits.