6.

$$\Psi^{-\infty}_{sm}(X) = \mathcal{A}(\mathbb{R}; \Psi^{-\infty}(X))$$

$$= C^\infty([-1,1] \times X^2)$$

(↑ commutative; ↖ non-commutative)

$$K^{-1}(Y) = [Y; G^{-\infty}_{sm}(X)]$$

Any smooth $\times$ $\det > 0$

$$G^{-\infty}_{sm}(X) = \{ Id + E;\ E \in \Psi^{-\infty}_{sm}(X),$$

$$(Id+E)^{-1} \text{ exists} \}$$

$$c_0 : K^{-1}(Y) \longrightarrow \mathbb{Z}$$

$$c : K^{-1}(Y) \longrightarrow H^{\text{even}}(Y)$$

$$c_0 = \frac{1}{2\pi i} \int_{-\infty}^{\infty} \mathrm{Tr}\left(f^{-1} \frac{\partial}{\partial s} f\right) ds$$

$$= \frac{1}{2\pi i} \mathrm{Tr}_\Sigma \left(f^{-1} \frac{1}{\partial_t} f\right)$$

$$\mathrm{ind}(P) = c_0(Id + E(\xi)).$$