12.

$$\mathcal{L} \downarrow$$

$$A^{\infty}_{\mathrm{LSU}}(\mathcal{H}) = G^{\infty}_{\mathrm{LSU}}(\mathcal{H}) \Big/ G^{-\infty}_{\mathrm{LSU}}(\mathcal{H})$$

A complex line bundle.

A determinant exists

$\Leftrightarrow$ $\mathcal{L}$ is trivial. (It isn't).

- $\Psi^{0}_{\mathrm{LSU}}(\mathcal{H})$ has a unique trace, Tr_R

  [Wodzicki, Guillemin, Byhuttchi–Gutzyler].

  "residue trace" descends to $A^{\infty}_{\mathrm{LSU}}(\mathcal{H})$

- $\mathrm{Tr}: \Psi^{-\infty}_{\mathrm{LSU}}(\mathcal{H}) \to \mathbb{C}$ has an extension

  $\overline{\mathrm{Tr}}_H : \Psi^{0}_{\mathrm{LSU}}(\mathcal{H}) \to \mathbb{C}$ <u>not</u> a trace.

$$\overline{\mathrm{Tr}}_H([A,B]) = \mathrm{Tr}_R(B D_H A)$$

← Exterior derivative