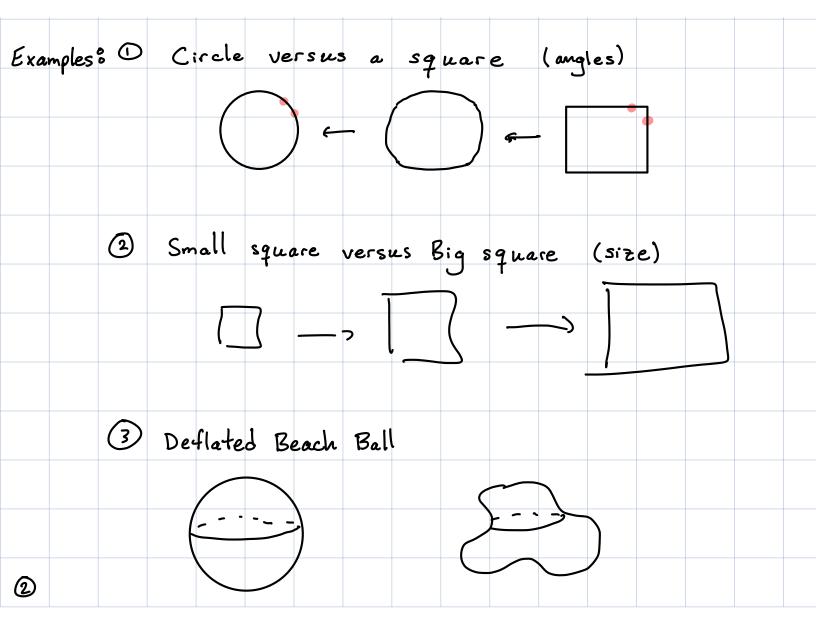
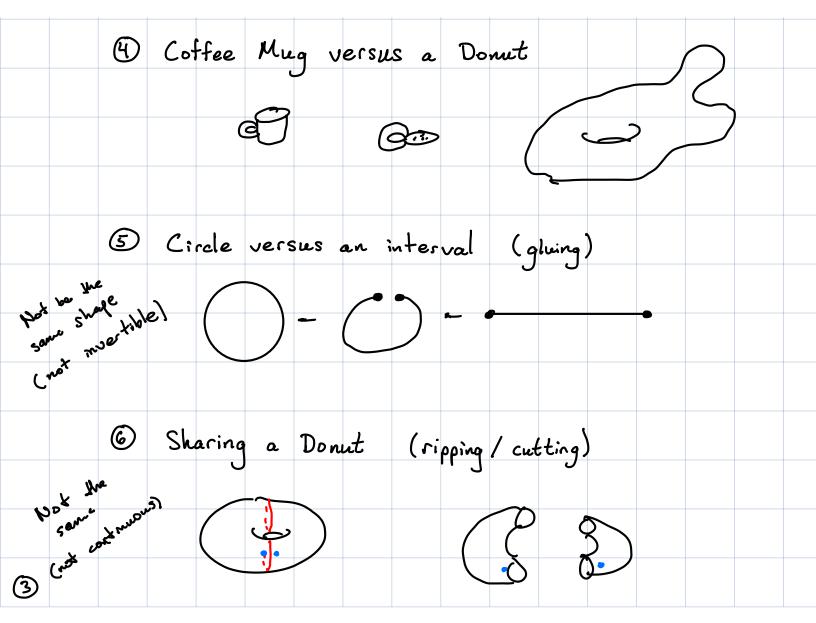
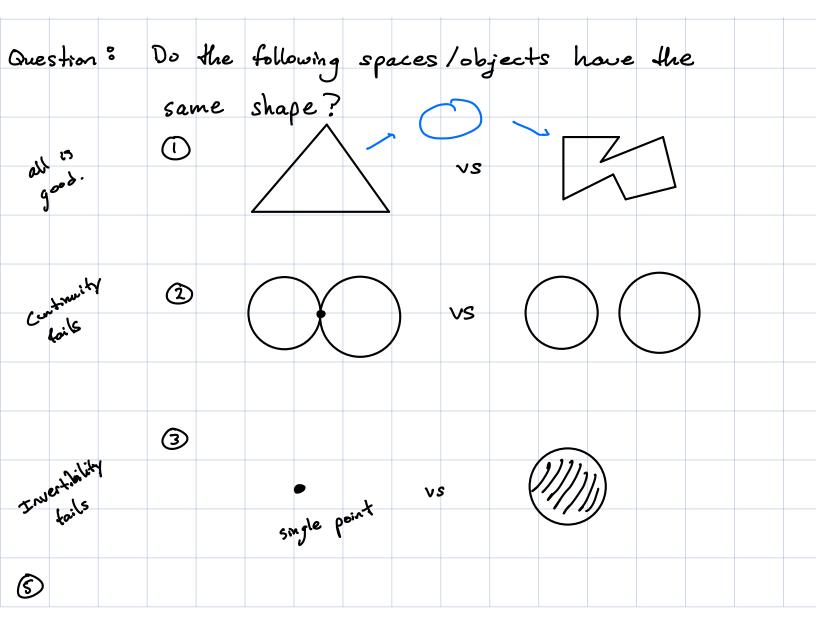
Lecture # 1 8 An Introduction Remark: Topus = shape Topology = the study of SHAPE ology = the study of J Question: What does it mean for things to have the same shape? Two objects have the same shape if we can Answers continuously deform ) rearrange , b in one objeto get the pts in other object.  $\bigcirc$ 

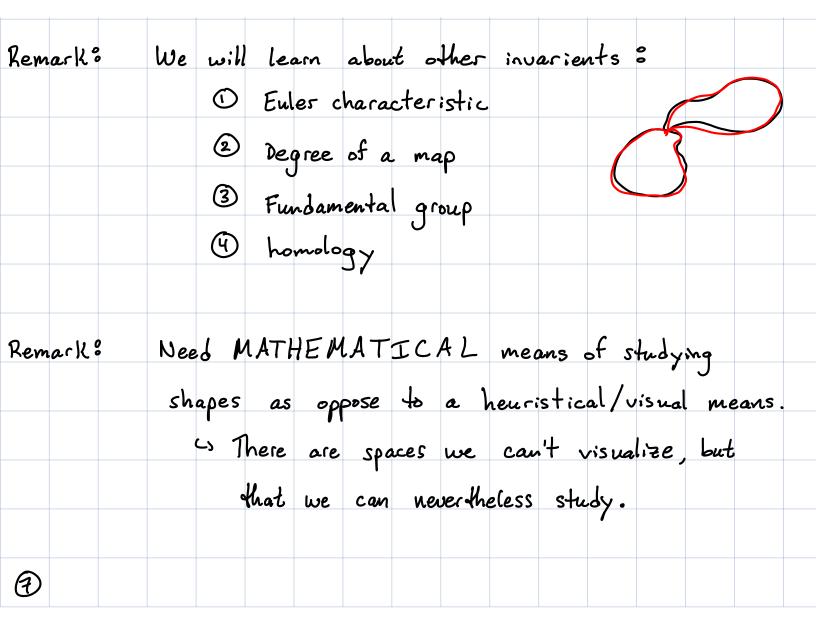




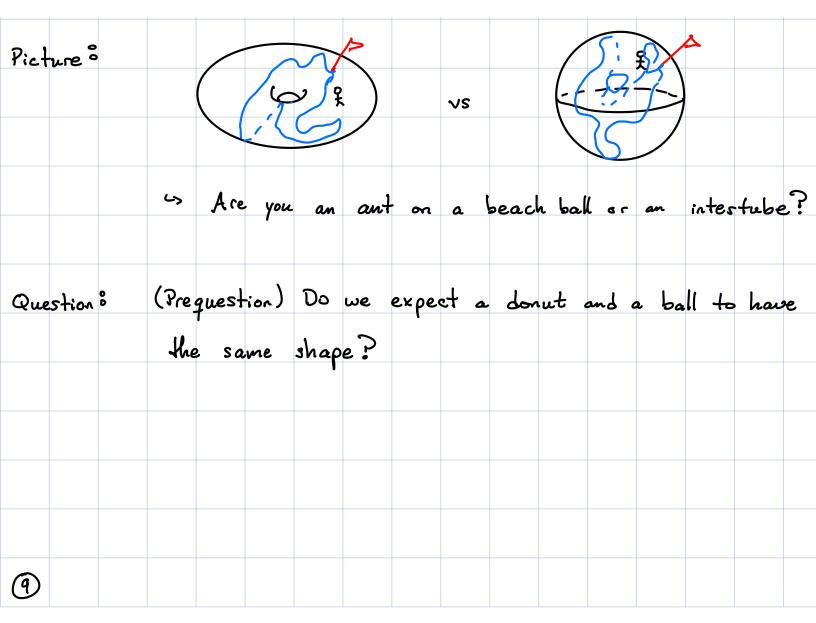
Remark: Two objects have the same shape if these deformings / rearrangings that relate them are 1) Invertible -> There is a way of undoing the rearrangement such that every point goes back to where it started. 2) Continuous " The rearrangement takes points that are infinitesimally close together to points that are infintesimally close together

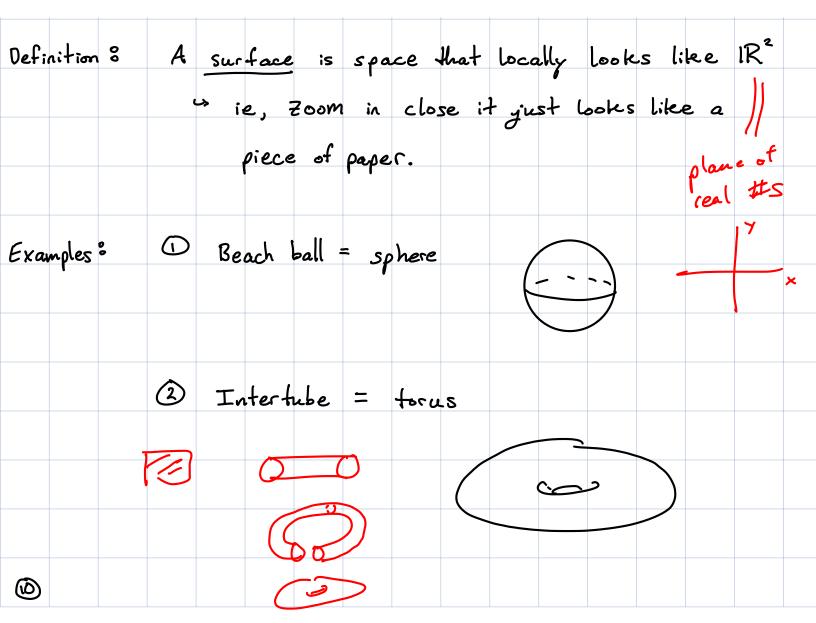


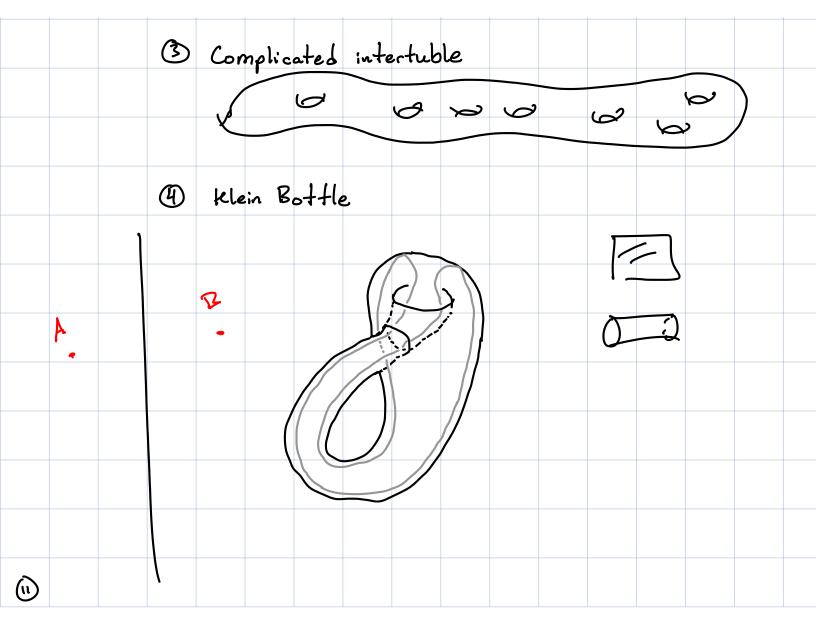
If two objects have the same shape, Definition 8 then we say that they are homeomorphic Topologists try to create invarients of spaces that Remark 8 detect differences in shape. Space numbers space algebraic obj. The # of connected pieces/components Example ° L> If different # of pieces, then not 6 homeomorphic.

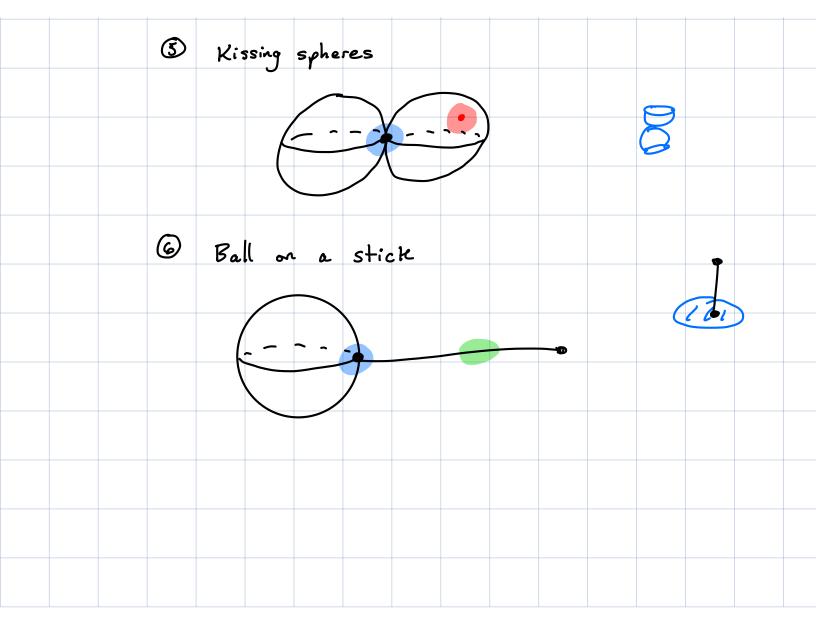


(A thought experiment) Aliens have abducted you Question : and your friends and transported you to an alternate universe for experimentation. However, the man w/ a cat who runs the universe prohibits experimentation on "logical" beings. Thus the aliens set up a task for you to complete. They drop you on a planet and ask you to deduce if the planet has the shape of a ball or a donut (the physical laws of the universe allow for this possibility). You may request and use any tools you want. However, the aliens have cloaked the planet so sutside observation ⑧ from outerspace is useless.









Topics Ahead: 1 The Four Colors Theorem 2 Classification of surfaces 3 Brouwer's Fixed Point Theorem ~ Nash? (4) Fundamental Theorem of algebra 5 Hairy Ball Theorem 6 Persistence and Topological Data Analysis Knot Theory Ŧ 8 Some other popular demand? 12