PROBLEM SET 14: ALTERNATING SERIES

Note: Most of the problems were taken from the textbook [1].

Problem 1. Test the series for convergence or divergence.

$$a) \sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{3+5n};$$

$$b) \sum_{n=1}^{\infty} \frac{(-1)^n n^2}{n^2 + n + 1};$$

$$c) \sum_{n=1}^{\infty} \frac{(-1)^n n}{e^n};$$

d)
$$\sum_{n=1}^{\infty} (-1)^{n-1} \tan^{-1}(n)$$
;

$$e) \sum_{n=1}^{\infty} \frac{n \cos \pi n}{2^n};$$

$$f) \sum_{n=1}^{\infty} (-1)^n \cos(\pi/n);$$

$$g) \sum_{n=1}^{\infty} (-1)^n \sin(\pi/n);$$

$$h) \sum_{n=1}^{\infty} (-1)^n \frac{n^n}{n!};$$

$$i) \sum_{n=1}^{\infty} (-1)^n (\sqrt{n+1} - \sqrt{n}).$$

Problem 2. Approximate the sum of the series correct to four decimal places.

$$a) \sum_{n=1}^{\infty} \frac{(-1)^n}{(2n)!};$$

$$b) \sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n^6};$$

c)
$$\sum_{n=1}^{\infty} \frac{(-1)^{n-1}}{n4^n}$$
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REFERENCES

[1] J. Stewart: Single Variable Calculus 8th Edition, Cengage Learning, Boston 2015.