DIRECTIONAL DERIVATIVES AND THE GRADIENT VECTOR

Problem 1. Let $f: \mathbb{R}^3 \to \mathbb{R}$ be a differentiable function, and let r(t), where $t \in [a, b]$, be a parametric curve in the domain of f. Show that vectors $\nabla f(r(t))$ and r'(t) are perpendicular for all $t \in [a, b]$.

References

[1] J. Stewart: Calculus 8th Edition, Cengage Learning, Boston 2016.