## PROBLEM SET 25: NONHOMOGENEOUS SECOND-ORDER LINEAR DIFFERENTIAL EQUATIONS

Note: Most of the problems were taken from the textbook [1].
Problem 1. Solve the differential equations.
a) $4 y^{\prime \prime}+2 y^{\prime}-8 y=1-2 x^{2}$;
b) $y^{\prime \prime}-4 y^{\prime}+4 y=x-\sin x$;
c) $9 y^{\prime \prime}+y=e^{2 x}$;
d) $y^{\prime \prime}-4 y^{\prime}+5 y=e^{-x}$.

Problem 2. Solve the initial-value problem.
a) $y^{\prime \prime}-2 y^{\prime}+5 y=\sin x, \quad y(0)=y^{\prime}(0)=1 ;$
b) $y^{\prime \prime}-y=x e^{2 x}, \quad y(0)=0, \quad y^{\prime}(0)=1$;
c) $y^{\prime \prime}+y^{\prime}-2 y=x+\sin 2 x, \quad y(0)=1, \quad y^{\prime}(0)=0$.

References
[1] J. Stewart: Single Variable Calculus 8th Edition, Cengage Learning, Boston 2015.

