## PROBLEM SET 23: LINEAR DIFFERENTIAL EQUATIONS

Note: Most of the problems were taken from the textbook [1].
Problem 1. Solve the differential equations.
a) $x y^{\prime}+y=\sqrt{x}$;
b) $t^{2} \frac{d y}{d t}+3 t y=\sqrt{1+t^{2}}, \quad t>0$.

Problem 2. Solve the initial-value problem.
a) $x^{2} y^{\prime}+2 x y=\ln x, \quad y(1)=2$;
b) $x y^{\prime}+y=x \ln x, \quad y(1)=0$;
c) $x y^{\prime}=y+x^{2} \sin x, \quad y(\pi)=0$.

## References

[1] J. Stewart: Single Variable Calculus 8th Edition, Cengage Learning, Boston 2015.

