

**September 27:** David Vogan (MIT), “The Langlands conjecture and covering groups (after Buzzard and Gee).”

Class field theory provides a bijection between “algebraic” characters of the idele class group of a number field  $F$ , and “compatible systems” of one-dimensional  $\ell$ -adic representations of the Galois group  $\text{Gal}(\overline{F}/F)$ . The Langlands conjecture, in a form made precise by Clozel in 1990, suggests a parallel relationship between “algebraic” automorphic forms for  $GL(n, F)$ , and compatible systems of  $n$ -dimensional  $\ell$ -adic representations of  $\text{Gal}(\overline{F}/F)$ . A recent preprint “The conjectural connection between automorphic representations and Galois representations,” by Kevin Buzzard and Toby Gee, discusses the extension of these conjectures to automorphic forms on a general reductive group  $G(F)$ . A basic question is how properly to define “algebraic.” What Buzzard and Gee argue is that there are *two* different interesting answers to this question, differing by a “rho shift.” I’ll explain their two definitions (called “L-algebraic” (for Langlands) and “C-algebraic” (for cohomological)).