

COMBINATORICS SEMINAR  
On The Maximum Number Of Edges In  
 $K$ -Quasi-Planar Graphs

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Abstract:

A topological graph is called  $k$ -quasi-planar, if it does not contain  $k$  pairwise crossing edges. It is conjectured that for every fixed  $k$  the maximum number of edges in a  $k$ -quasi-planar graph on  $n$  vertices is  $O(n)$ . We provide, for the first time, an affirmative answer to the case  $k = 4$ . We also give the simplest proof and the best upper bound known, for the maximum number of edges in 3-quasi-planar graphs on  $n$  vertices. Moreover, we show a tight upper bound for 3-quasi-planar graphs in which every pair of edges meet at most once.

Joint work with Gabor Tardos.