



Skeletal Structures and Origami Design

By Michelle Lau and Kaylee Xie



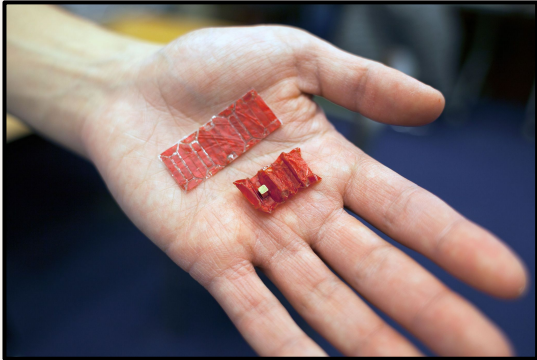
Table of contents:

01.....	Goals & Introduction
02	Terminology
03.....	Stick Figures
04.....	Claim
05.....	Circle Packing
06.....	Skeletal Structures
07.....	Uniaxial Base
08.....	Final Shape!

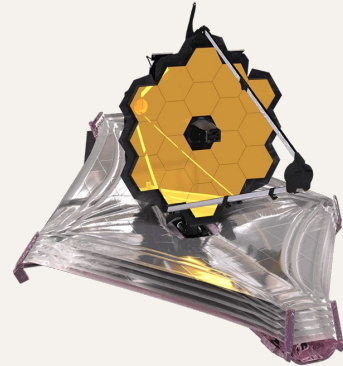
Why Origami?

Origami is a **real world application** of geometric principles that helps us construct physical structures.

Understanding **spatial and geometric intuition**



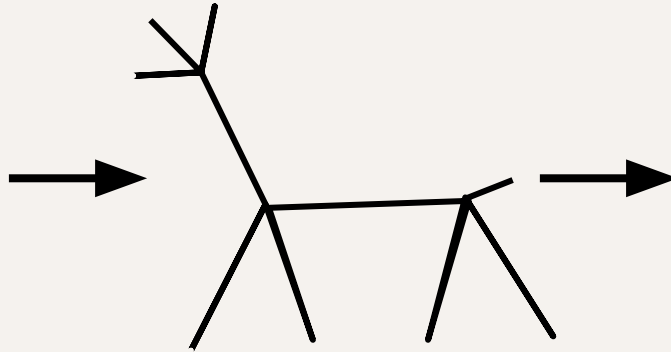
MIT's ingestible
origami robot



JWST unfolds
when in space

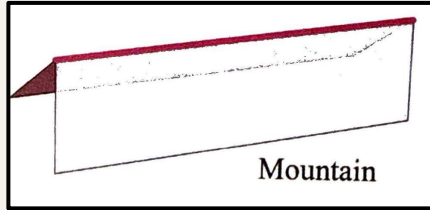
Objective

We want to take something **from an idea**
or concept into reality.

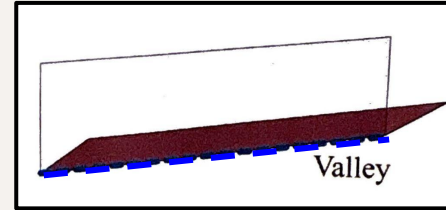


Terminology

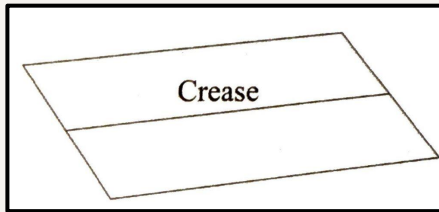
Mountain Fold



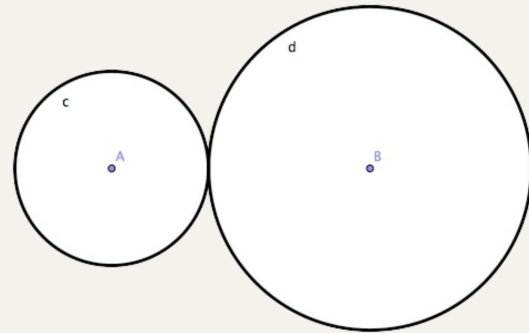
Valley Fold



Creases

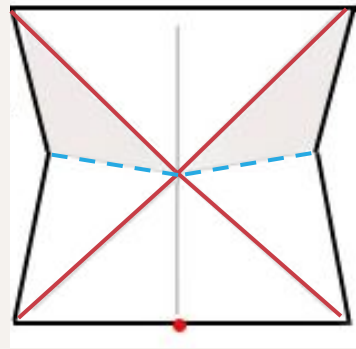
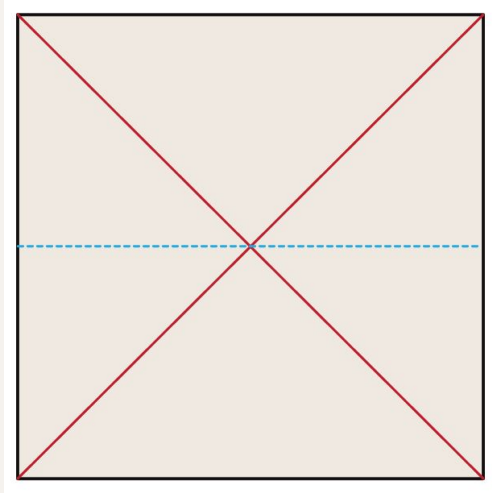


Tangent Circles

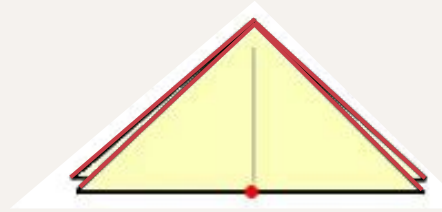


Terminology Applied

Base - a 2D diagram of the folds that create a structure



Final Folded Shape



RED = Mountain
Fold

BLUE = Valley Fold

Folds Flat

Stick Figures

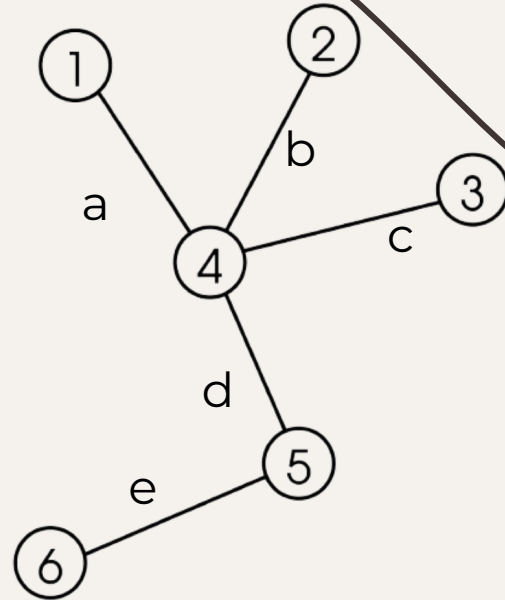
The **stick figure** is the basic frame, or “bones” of a structure.

It is represented by a **metric tree**

Metric Tree:

Tree → graph with no cycles

Metric → edges with lengths



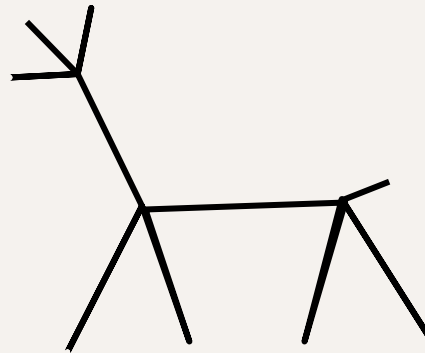
Vocab:

A **terminal edge**: line segment with 1 endpoint connected

Stick Figures

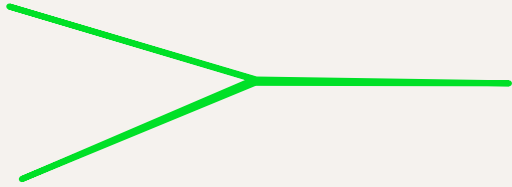
Think about a deer:

- What lines do you need to define it?

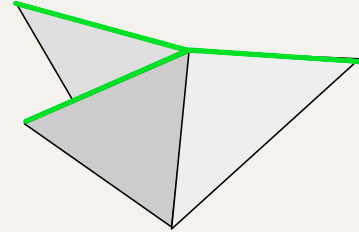
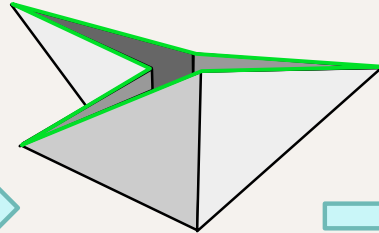
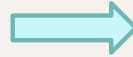
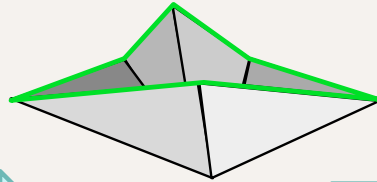
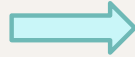
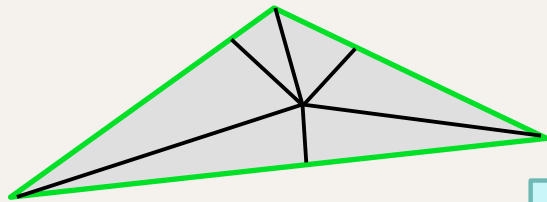


The stick figure for an origami deer as seen to the left, and the physical representation above.

Stick Figures \rightarrow 3D

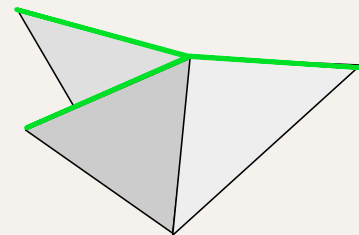
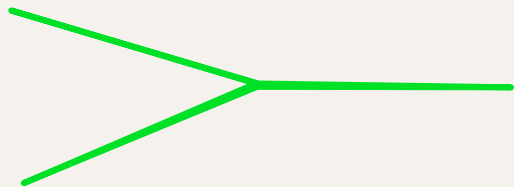


Stick figure \rightarrow Polygon that
props up stick figure

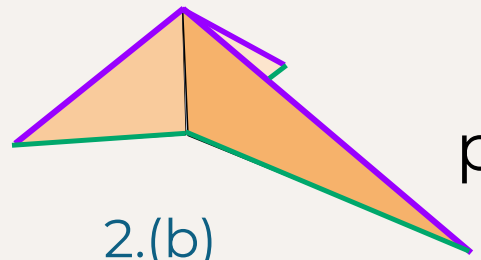
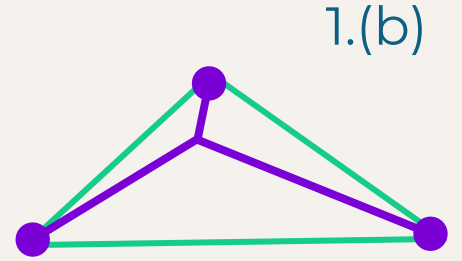
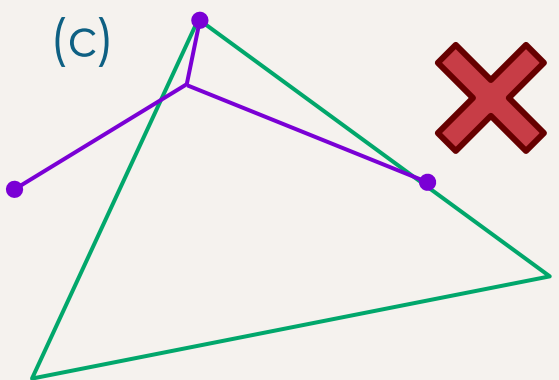
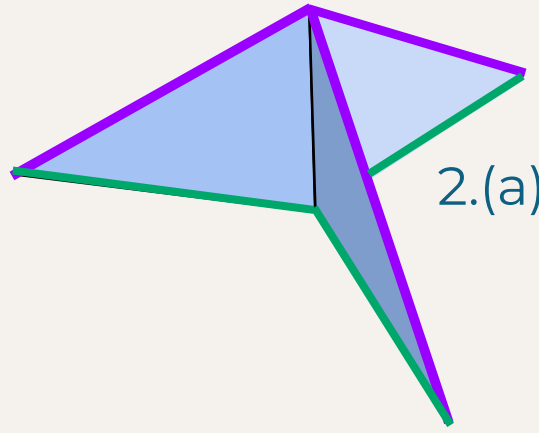
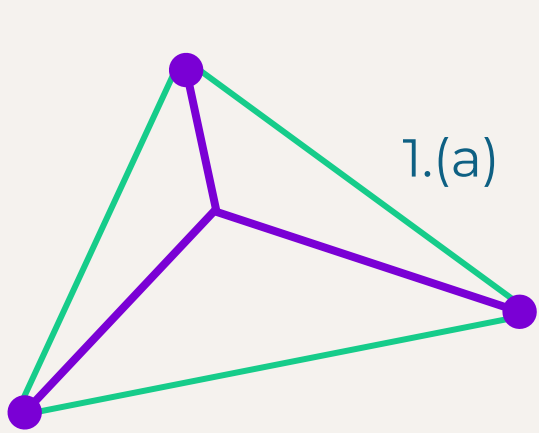


Claim

Given a stick figure, there is a base with a perimeter that creates the stick figure.



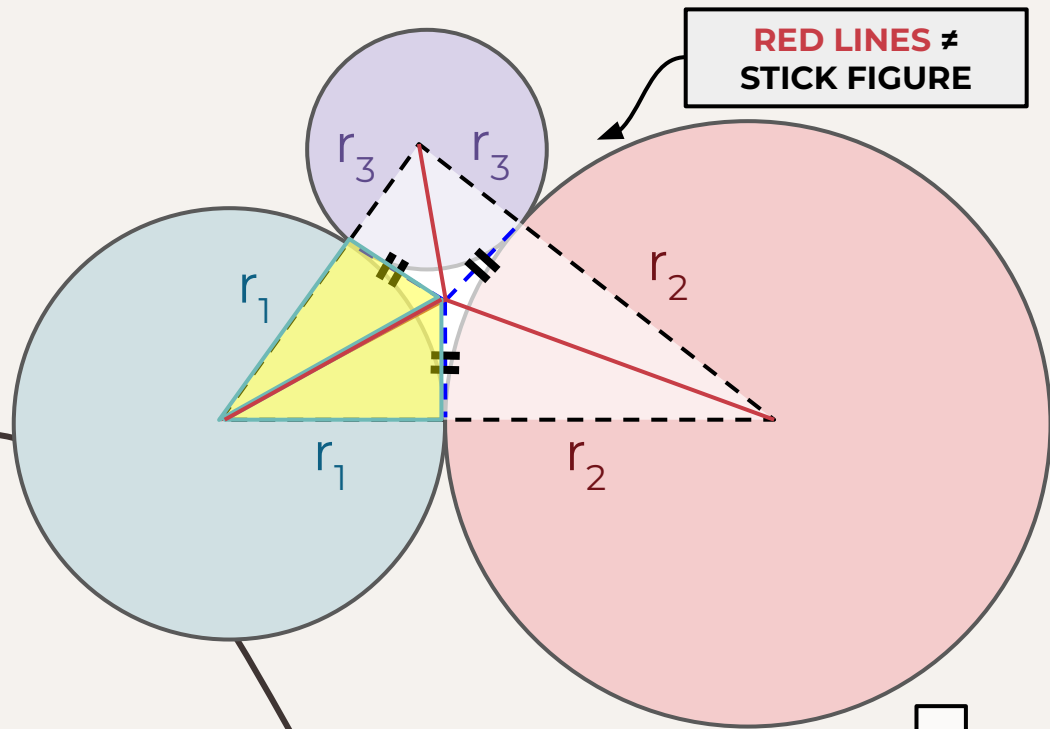
There are many stick figures that 'make' a triangle...



How do we find the polygon that recovers the given stick figure?

Circle packing

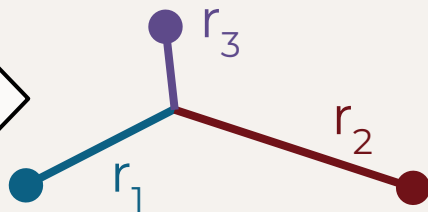
We are able to place circles centered at each vertex. Because the radii of the circles are the same length, this guarantees that the lengths will overlap correctly...



KEY

- || -> Represents congruent lengths
- - -> represents height from the middle point

STICK FIGURE

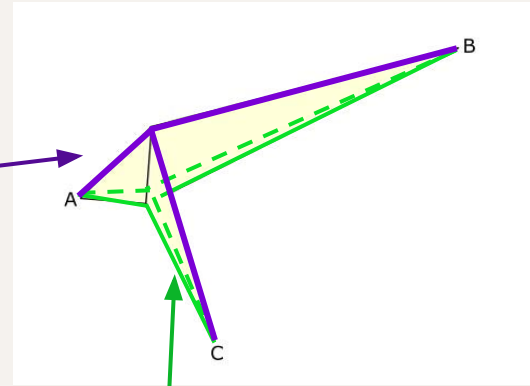


Creates stick figure with edge lengths r_1 , r_2 , and r_3

Skeletal Structure

The **skeletal structure** is the collection of **ridge creases**.

It is unique to each shape.

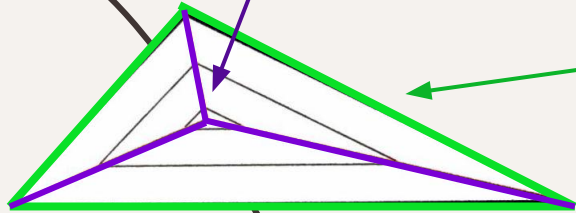


Purple lines make up the **skeletal structure**

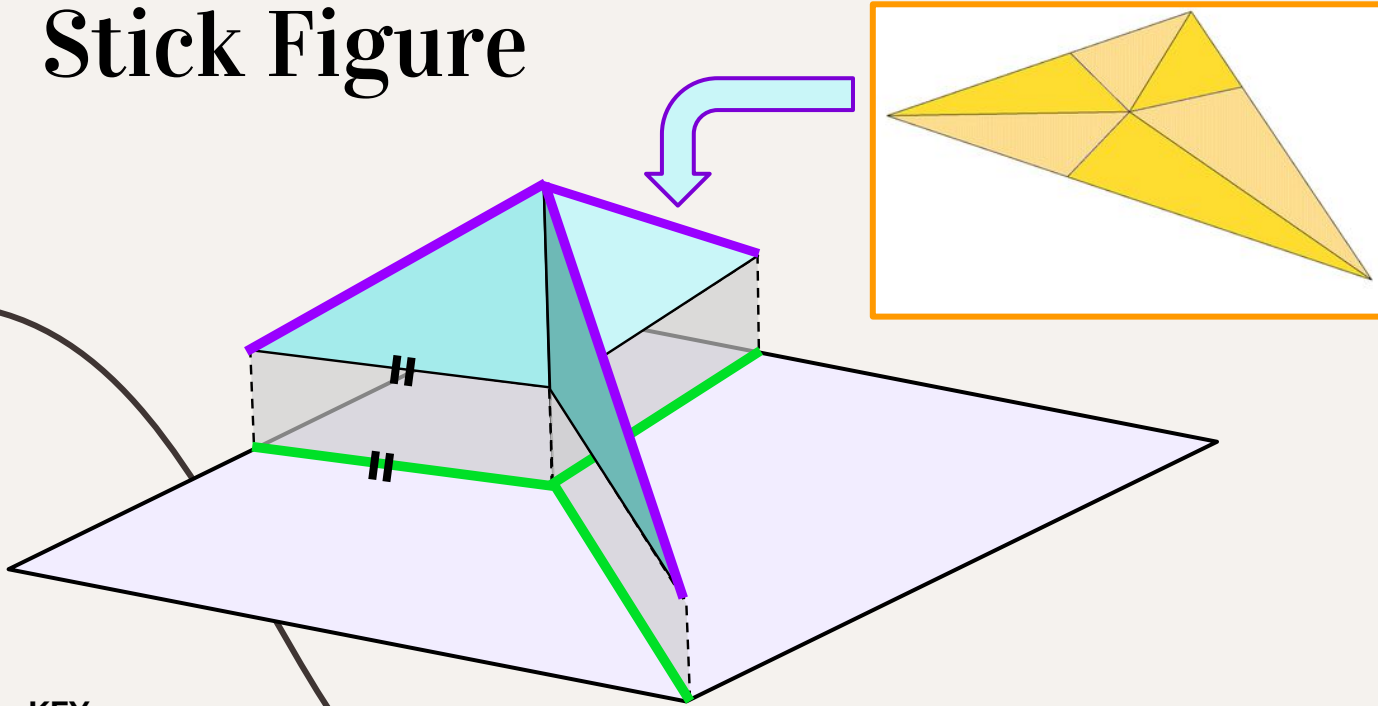
Green lines correspond to edges in **stick figure**

Definitions

Ridge creases = the lines/edges that extend from the plane of the stick figure



Skeletal Structure vs. Stick Figure



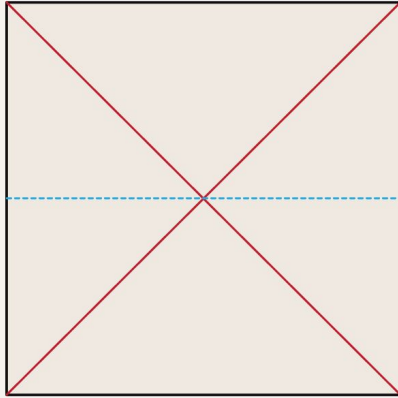
The **Skeletal Structure** consists of the **ridge creases** in a structure.

On the other hand, the **Stick Figure** is made from the **edges/perimeter** of the polygon folding together.

KEY

 -> Represents **Stick Figure**  -> Represents **Skeletal Structure**

Uniaxial Base



The Waterbomb Base is an example of a uniaxial base.

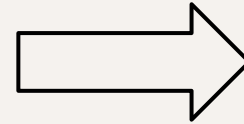
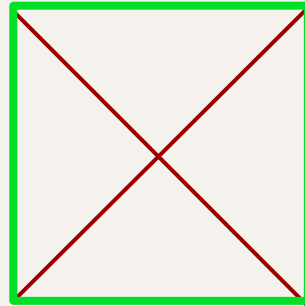
RED = Mountain Fold

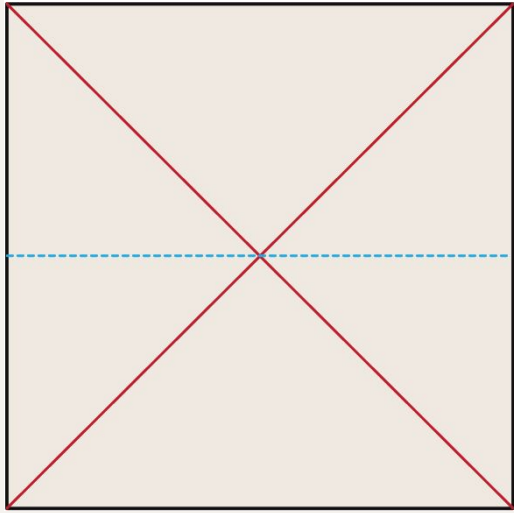
BLUE = Valley Fold

Reminder!

Base - a 2D diagram of the folds to create a structure

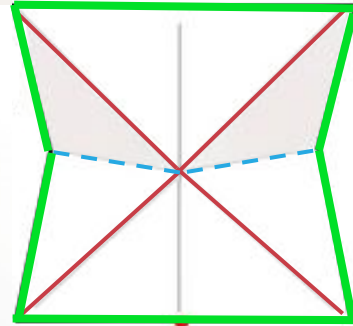
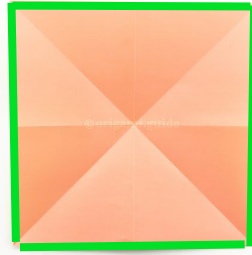
A base where the stick figure, or perimeter of the base, flat folds onto a **single** axis.





Uniaxial Base

This shows how the perimeter folds onto one axis.

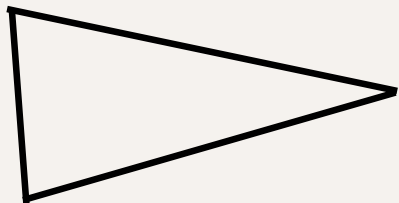


This is the bird's eye perspective of the base

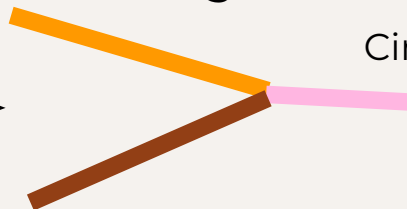
Final Shape!

This method can be used to create more complex bases, leading to a 3D representation of your stick figure!

Original shape

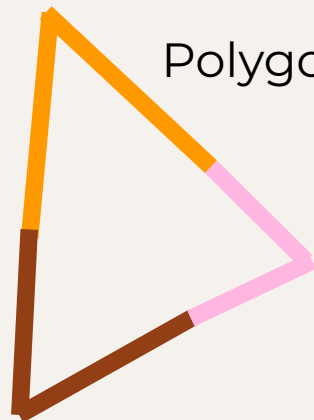


Stick figure

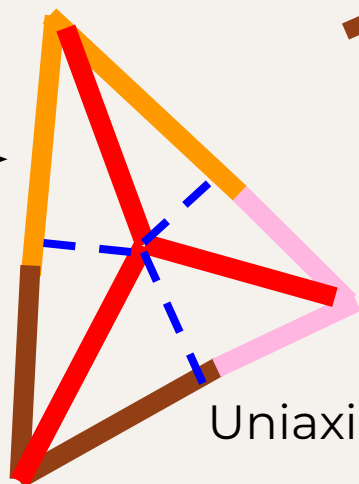


Circle Packing Method

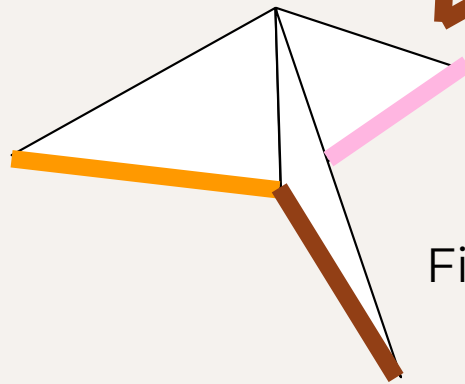
Polygon



Skeletal structure
and crease
pattern

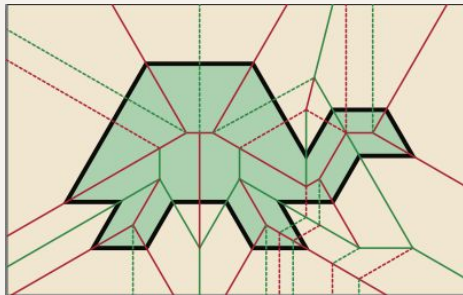
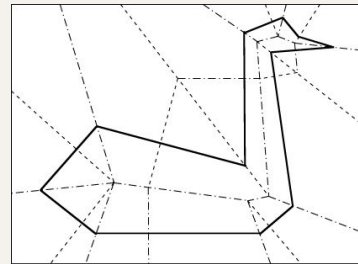


Fold!



Final Shape!

**Thank you for
listening!**



Sources:

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