

October 31: Kyo Nishiyama (Aoyama Gakuin University and MIT), “Generalized Steinberg maps and exotic moment maps for symmetric pairs.”

Let G be a reductive algebraic group. Steinberg established a map from the Weyl group to nilpotent G -orbits using moment maps on double flag varieties. In particular, in the case of the general linear group, he re-interpreted the Robinson-Schensted correspondence, which is combinatorial in its nature, in terms of the geometry of complete flags.

We generalize Steinberg’s theory to the case of symmetric pairs (G, K) , and obtained two different maps. They are called a “generalized Steinberg map” and an “exotic moment map”.

We explain what are these maps in the case where $(G, K) = (\mathrm{GL}_{2n}, \mathrm{GL}_n \times \mathrm{GL}_n)$. Unlike Steinberg, we start from geometry and then deduce combinatorial algorithms to describe generalized Steinberg maps and exotic moment maps. This amounts to establish a generalization of RS correspondence and an amusing relative for signed Young diagrams.

This is an on-going joint work with Lucas Fresse (IECL, University of Lorraine).