

### **Tobias Holck Colding: Publications**

1. T.H. Colding and W.P. Minicozzi II, Quantitative uniqueness for mean curvature flow, *Journal of Mathematical Study*, to appear.
2. T.H. Colding and W.P. Minicozzi II, Gradient estimates for scalar curvature, preprint.
3. T.H. Colding, Weak solutions in the sense of Calabi, in "The legacy of Eugenio Calabi (1923-2023)", *Notices of the AMS*, Volume 71, Number 11, 1502-1520, December 2024.
4. T.H. Colding and W.P. Minicozzi II, Minimal Submanifolds, *Encyclopedia of Mathematical Physics (Second Edition) Volume 1*, 2025, Pages 402–417.
5. T.H. Colding and W.P. Minicozzi II, A strong Frankel theorem for shrinkers, *Compositio Mathematica*, to appear.
6. T.H. Colding and W.P. Minicozzi II, Eigenvalue lower bounds and splitting for modified Ricci flow, *Advanced Nonlinear Studies*, 24 (2024), no. 1, 178–188.
7. T.H. Colding and W.P. Minicozzi II, Propagation of symmetries for Ricci shrinkers, *Advanced Nonlinear Studies*, 23 (2023), no. 1, ans-2022–0071.
8. T.H. Colding and W.P. Minicozzi II, Jesse Douglas, *Biographical Memoirs of the National Academy of Sciences*,  
[https://www.nasonline.org/wp-content/uploads/2024/10/Douglas\\_Jesse.pdf](https://www.nasonline.org/wp-content/uploads/2024/10/Douglas_Jesse.pdf).
9. T.H. Colding and W.P. Minicozzi II, Singularities and diffeomorphisms, *Notices of the International Consortium of Chinese Mathematicians*, Vol. 10, No. 1 (2022), 112–116.
10. T.H. Colding, Evolution of form and shape, *ICM–International Congress of Mathematicians. Vol. II. Plenary lectures*, 826–871, EMS Press, Berlin, [2023], 2023.
11. T.H. Colding and W.P. Minicozzi II, Singularities of Ricci flow and diffeomorphisms, preprint.
12. T.H. Colding and W.P. Minicozzi II, Parabolic frequency on manifolds, *Int. Math. Res. Not. IMRN* 2022, no. 15, 11878–11890.
13. T.H. Colding and W.P. Minicozzi II, In search of stable geometric structures, *Notices of the AMS*, Vol. 66, no. 11 (2019) 1785–1791.
14. T.H. Colding and W.P. Minicozzi II, Regularity of elliptic and parabolic systems, *Annales scientifiques de l’Ecole normale supérieure*, (4) 56 (2023), no. 6, 1883–1921.

15. T.H. Colding and W.P. Minicozzi II, Complexity of parabolic systems, Publ. Math. Inst. Hautes Etudes Sci. 132 (2020) 83–135.
16. T.H. Colding and W.P. Minicozzi II, Liouville properties, ICCM Not. 7 (2019), no. 1, 16–26.
17. T.H. Colding, D. Gabai, and D. Ketover, Geometric methods in Heegaard theory (with appendix by T.H. Colding and D. Gabai), Surveys in Differential Geometry, Vol. 25, No. 1 (2020), 33–70.
18. T.H. Colding and W.P. Minicozzi II, Optimal bounds for ancient caloric functions, Duke Math. J. 170 (2021), no. 18, 4171–4182.
19. T.H. Colding and W.P. Minicozzi II, Wandering singularities, J. Differential Geom., 119 (2021) 403 – 420.
20. T.H. Colding and W.P. Minicozzi II, Dynamics of closed singularities, Annales de l’Institut Fourier, Tome 69 (2019) no. 7, 2973–3016.
21. T.H. Colding and W.P. Minicozzi II, Analytical properties for degenerate equations. Geometric Analysis, In Honor of Gang Tian’s 60th Birthday, Progress in Mathematics series by Birkhauser. Editors: Jingyi Chen, Peng Lu, Zhiqin Lu, and Zhou Zhang, Vol. 333, (2020) 57–70.
22. T.H. Colding and W.P. Minicozzi II, Arnold-Thom gradient conjecture for the arrival time, Comm. Pure and Appl. Math, 72 (2019), no. 7, 1548–1577.
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26. T.H. Colding and W.P. Minicozzi II, Committee ranking, preprint.
27. T.H. Colding, D. Gabai and D. Ketover, On the classification of Heegaard splittings, Duke Math. J., Vol. 167, No. 15 (2018) 2833–2856.
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29. T.H. Colding and D. Gabai, Effective Finiteness of irreducible Heegaard splittings of non Haken 3-manifolds, Duke Math. J., Vol. 167, No. 15 (2018) 2793–2832.

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