# Homework Assignment 4 <br> Due April 14 <br> 18.952 

Problem 1, Section 4.1, exercises $7-12$
Problem 2, Exercises:

1. In section 4.1, exercise 8 , let $A_{t} \in S_{n}$ be a family of linear mappings depending smoothly on $t$ and satisfying $A_{t}^{2}=A_{t}$. Show that if $A_{0}=A$ and $B=\frac{d}{d t} A_{t}(t=0)$ then $B A+A B=B$.
2. Conclude from this that if $V$ is the kernel of $A$ and $W$ the kernel of $I-A$, then $B$ maps $V$ into $W$ and $W$ into $V$.
3. Let $\langle v, w\rangle$ be the Euclidean inner product on $\mathbb{R}^{n}$. Show that since $B$ is in $S_{n},\langle B v, w\rangle=\langle v, B w\rangle$ for all $v \in V$ and $w \in W$, and conclude that $B$ is determined by its restitution to $V$.
4. Show that if $A$ is in $G(k, n)$, the tangent space to $G(k, n)$ at $A$ is $\operatorname{Hom}(V, W)$.
