

Homework 2

18.086

Spring 2006

for FRIDAY 3/3/06

Combine numerical experiments with analysis for \*ONE\* of these PDE's:

**1.**  $\mathbf{u}_t = \mathbf{c} \mathbf{u}_x + \mathbf{d} \mathbf{u}_{xx}$  Create the “Figure 5.12” described in the notes and test “implicit diffusion” with  $d\Delta^2 U$  at time  $n + 1$ .

**2.**  $\mathbf{u}_t = \mathbf{i} \mathbf{u}_{xx}$  (*Schrödinger's equation*) Stability conditions for explicit and implicit; examples and code.

**3.**  $\mathbf{u}_t = \mathbf{c} \mathbf{u}_x$  Use the website code or your own to compare upwind–LF–LW–leapfrog for different  $r = c\Delta t/\Delta x$ . How does the Lax-Wendroff oscillation depend on  $r$ ? Does the solution from a step function approach a steady profile? What is width  $W\Delta x$  of the discrete shock in each method?

**4.**  $\mathbf{u}_t = \mathbf{u} \mathbf{u}_x$  (*Conservation law*) Write a code to test upwind vs. Lax-Wendroff on examples when shocks or fans form. Refer to 16.920 notes on [ocw.mit.edu](http://ocw.mit.edu).