

2012 Integration Bee Solutions

$$\text{int1. } 2 \log(\sqrt{x} - 1) + 2\sqrt{x}$$

$$\text{int2. } (4x^{5/4} \log(x))/5 - 16x^{5/4}/25$$

$$\text{int3. } 2(\sqrt{x} - 1)/\sqrt{1-x}$$

$$\text{int4. } -(9\sqrt[4]{x} + 1)/\left(18(\sqrt[4]{x} + 1)^9\right)$$

$$\text{int5. } \pi/4$$

$$\text{int6. } \sin^{-1}\left((x+2)/\sqrt{5}\right)$$

$$\text{int7. } 1/12$$

$$\text{int8. } 1$$

$$\text{int9. } 1005$$

$$\text{int10. } 2 \tan^{-1} \sqrt{x + \frac{1}{x} + 1}$$

$$\text{int11. } 33/2 - 24 \log(2)$$

$$\text{int12. } \sin(x) \log(x)$$

$$\text{int13. } \log \sqrt{1 - 1/x^2}$$

$$\text{int14. } 1/2 - \pi\sqrt{3}/12$$

$$\text{int15. } 1/10100$$

$$\text{int16. } 4/3$$

$$\text{int17. } 6x^{1/6} - 6 \tan^{-1}(x^{1/6})$$

$$\text{int18. } (\log(x + \sqrt{x^2 - 1/2}))/\sqrt{2}$$

$$\text{int19. } 2 \tan^{-1} \sqrt{e^x - 1} \text{ or } -2 \sin^{-1} e^{-x/2}$$

$$\text{int20. } \frac{1}{4} \tan^{-1}(x^2/2)$$

$$\text{int21. } (\cos(x) + \sin(x))/(\cos(x) - \sin(x)) \text{ or } \tan(x + \pi/4)$$

int22. $\log \tanh(x/2) - x/\sinh(x)$

int23. $1192/45$

int24. $\log 8 = 3 \log 2$

int25. $2\sqrt{\sin(x)}$