# Quantitative Reasoning 28: <br> The Magic of Numbers 

## Homework 25

## Assigned on Monday November 24th <br> Due at 12 noon Wednesday November 26th

Please submit problem sets at the end of the relevant lecture, or leave in the box labeled QR28 outside the Math Department's main office, on the third floor of the Science Center (Room 325).

## Reading:

Gross-Harris, Chapter 20

## Problems:

Please explain your reasoning and show your work.

1. (a) Compute $3^{917}(\bmod 140)$.
(b) Compute $4^{1125}(\bmod 105)$.
2. The method we have used for computing roots $(\bmod n)$ can be applied to only part (c) of the following three problems. Explain why it fails for the first two problems, and solve the third.
(a) The 4 th root of $4(\bmod 77)$;
(b) The 7 th root of $7(\bmod 77)$;
(c) The 13 th root of $13(\bmod 77)$.
3. (a) Compute the 11 th root of $2(\bmod 105)$.
(b) Compute the 5 th root of $4(\bmod 39)$.
