Topological Defects 18.5995 - LI3

Order Parameters, Broken Symmetry, and Topology

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Topological defects are discontinuities in order-parameter fields



- optical effects
- work hardening, etc



"umbilic defects" in a nematic liquid crystal

order = symmetry = invariance (under certain group actions)

symmetry groups can be discrete, continuous, Lie-groups,

More or less symmetric ?



More or less symmetric ?



 $Mg_2Al_4Si_5O_{18}$





More or less symmetric ?

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B

broken continuous translation/rotation symmetry (invariance)

Order parameters: 2D crystal





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$$\vec{u} \equiv \vec{u} + a\hat{x} = \vec{u} + ma\hat{x} + na\hat{y}.$$

$$\mathcal{E} = \int dx \, (\kappa/2) (du/dx)^2.$$

Order parameters: magnets



Order parameters: nematic liquid crystals



"projective plane" = half-sphere with opposite points on equator identified

Topological defects









Work hardening





Disclinations





Disclineations









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e

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Dislocation-mediated growth of bacterial cell walls

Ariel Amir and David R. Nelson¹



PNAS | June 19, 2012 | vol. 109 | no. 25 | 9833-9838

Bacterial vortices





Microtubule asters



Active nematics



Dogic lab (Brandeis) Nature 2012





Active nematics





Giomi et al PRL 2012



Defects in nematics







Defects in nematics



winding number





Two-Dimensional Nematic Colloidal Crystals Self-Assembled by Topological Defects

Igor Musevic *et al. Science* **313**, 954 (2006); DOI: 10.1126/science.1129660



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Reconfigurable Knots and Links in Chiral Nematic Colloids Uros Tkalec *et al.*

Science **333**, 62 (2011); DOI: 10.1126/science.1205705

