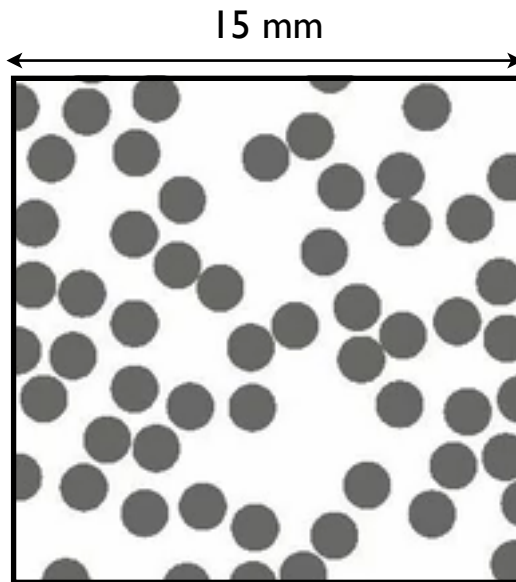


Reminder: last class

Kepler's 3 laws

3-body problem

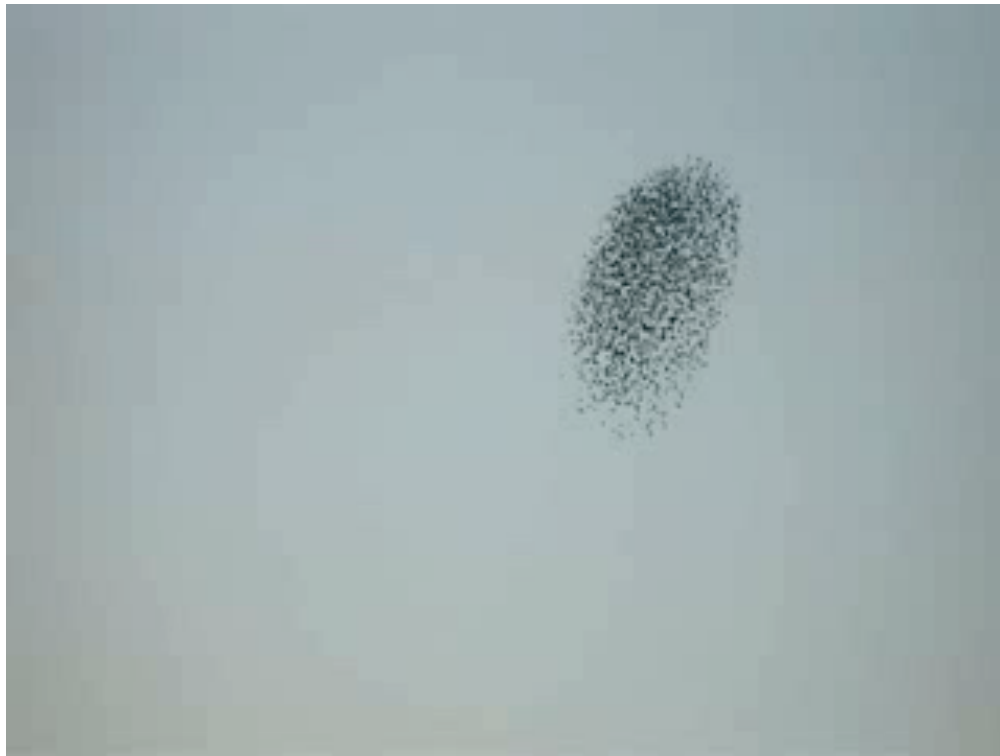


Dilute Fluid

$$\phi = 0.34$$

Molecular Dynamics Simulations

How do we describe systems with large N of particles?



Falcon attacks a flock of starlings

How do we describe systems with large N of particles?



Swarming:



How do we describe systems with large N of particles?



Traffic flow:

How do we describe systems with large N of particles?



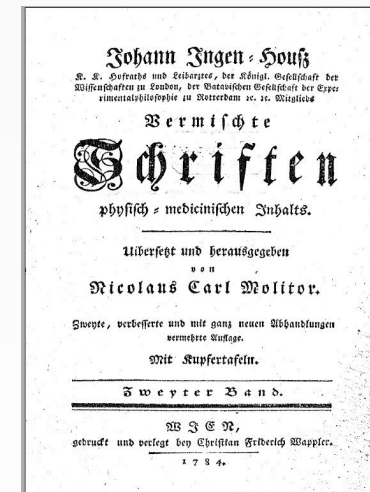
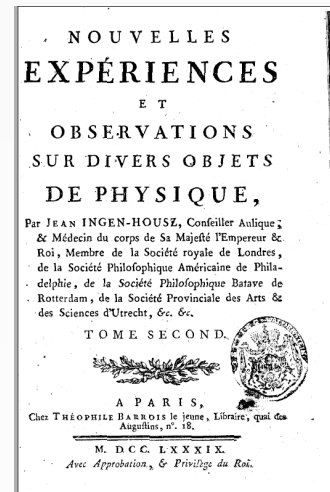
1st example: Brownian motion

Brownian motion



“Brownian” motion

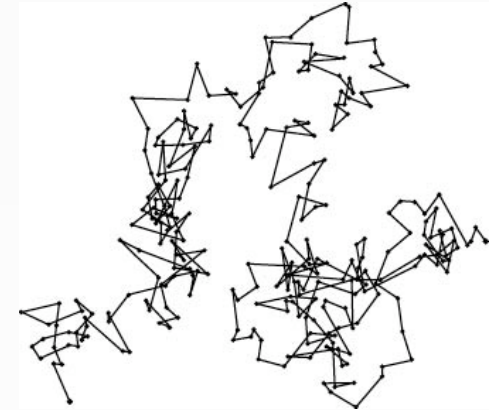
Jan Ingen-Housz (1730-1799)



1784/1785:

über betrügen könnte, darf man nur in den Brennpunct eines Mikroskops einen Tropfen Weingelst sammt etwas gestoßener Kohle setzen; man wird diese Körperchen in einer verwirrten beständigen und heftigen Bewegung erblicken, als wenn es Thierchen wären, die sich reißend unter einander fortbewegen.

Robert Brown (1773-1858)

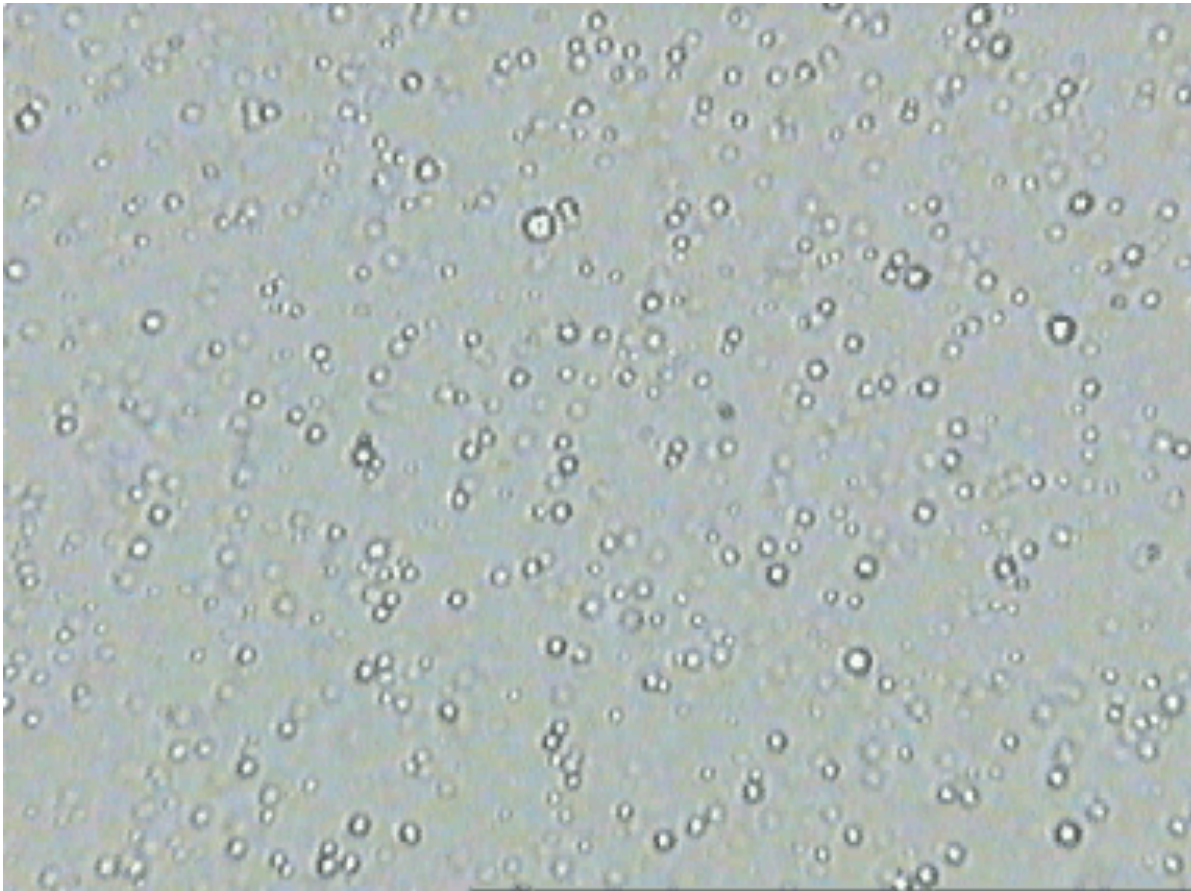


Linnean Society (London)

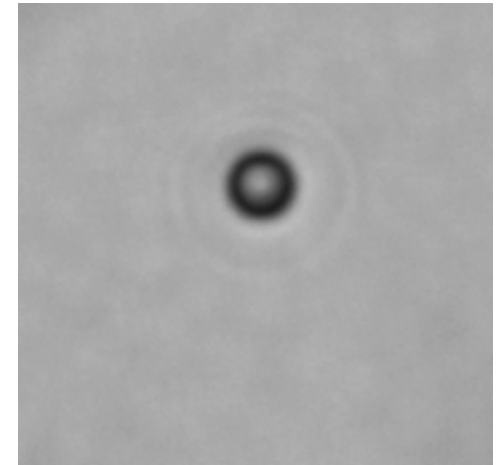
1827: irregular motion of pollen in fluid

<http://www.brianjford.com/wbbrownc.htm>

Brownian motion

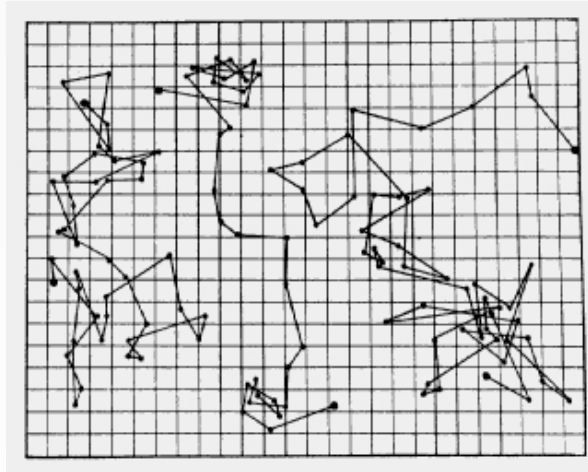
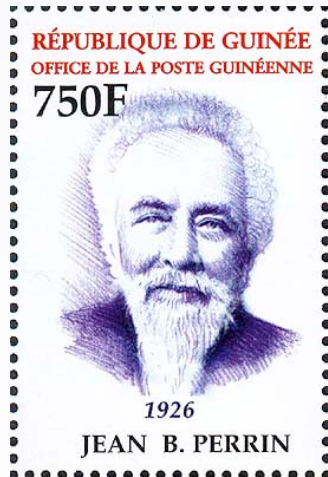


David Walker



Mark Haw

Jean Baptiste Perrin (1870-1942, Nobel prize 1926)



- ▶ colloidal particles of radius $0.53\mu\text{m}$
- ▶ successive positions every 30 seconds joined by straight line segments
- ▶ mesh size is $3.2\mu\text{m}$

Mouvement brownien et réalité moléculaire, Annales de chimie et de physique VIII 18, 5-114 (1909)

Les Atomes, Paris, Alcan (1913)

experimental evidence for
atomistic structure of matter

Theory of Brownian Motion

W. Sutherland (1858-1911)

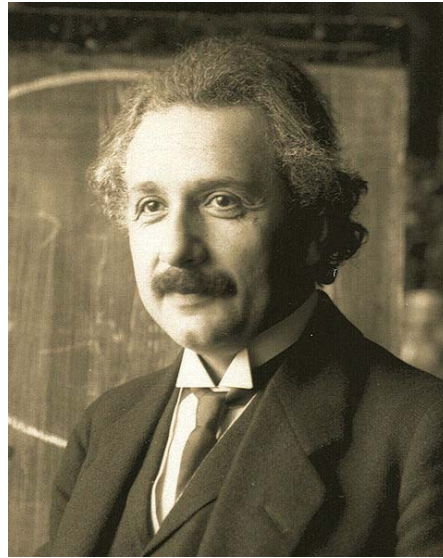


Source: www.theage.com.au

$$D = \frac{RT}{6\pi\eta aC}$$

Phil. Mag. **9**, 781 (1905)

A. Einstein (1879-1955)



Source: wikipedia.org

$$\langle x^2(t) \rangle = 2Dt$$

$$D = \frac{RT}{N} \frac{1}{6\pi kP}$$

Ann. Phys. **17**, 549 (1905)

M. Smoluchowski
(1872-1917)



Source: wikipedia.org

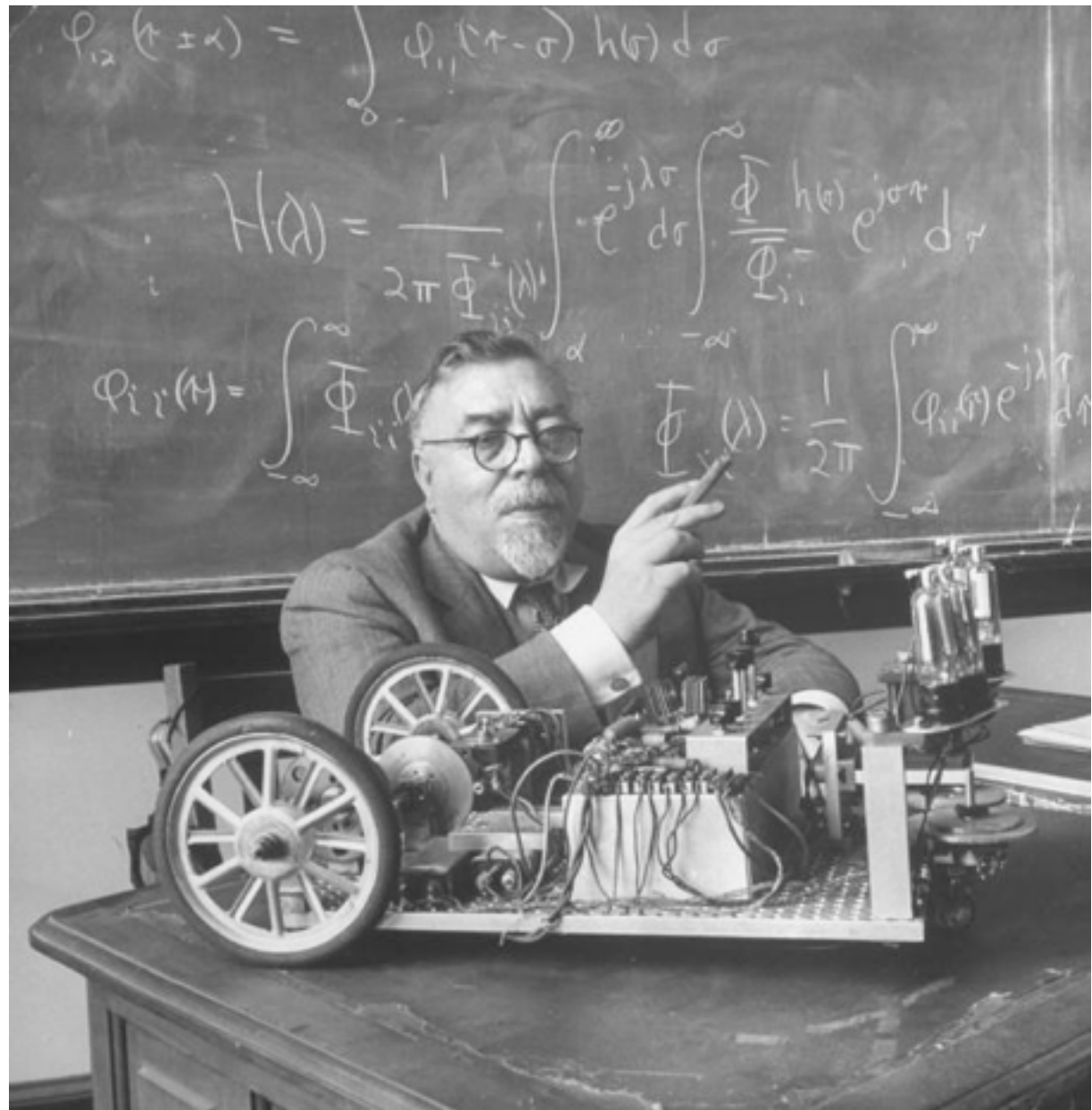
$$D = \frac{32}{243} \frac{mc^2}{\pi\mu R}$$

Ann. Phys. **21**, 756 (1906)

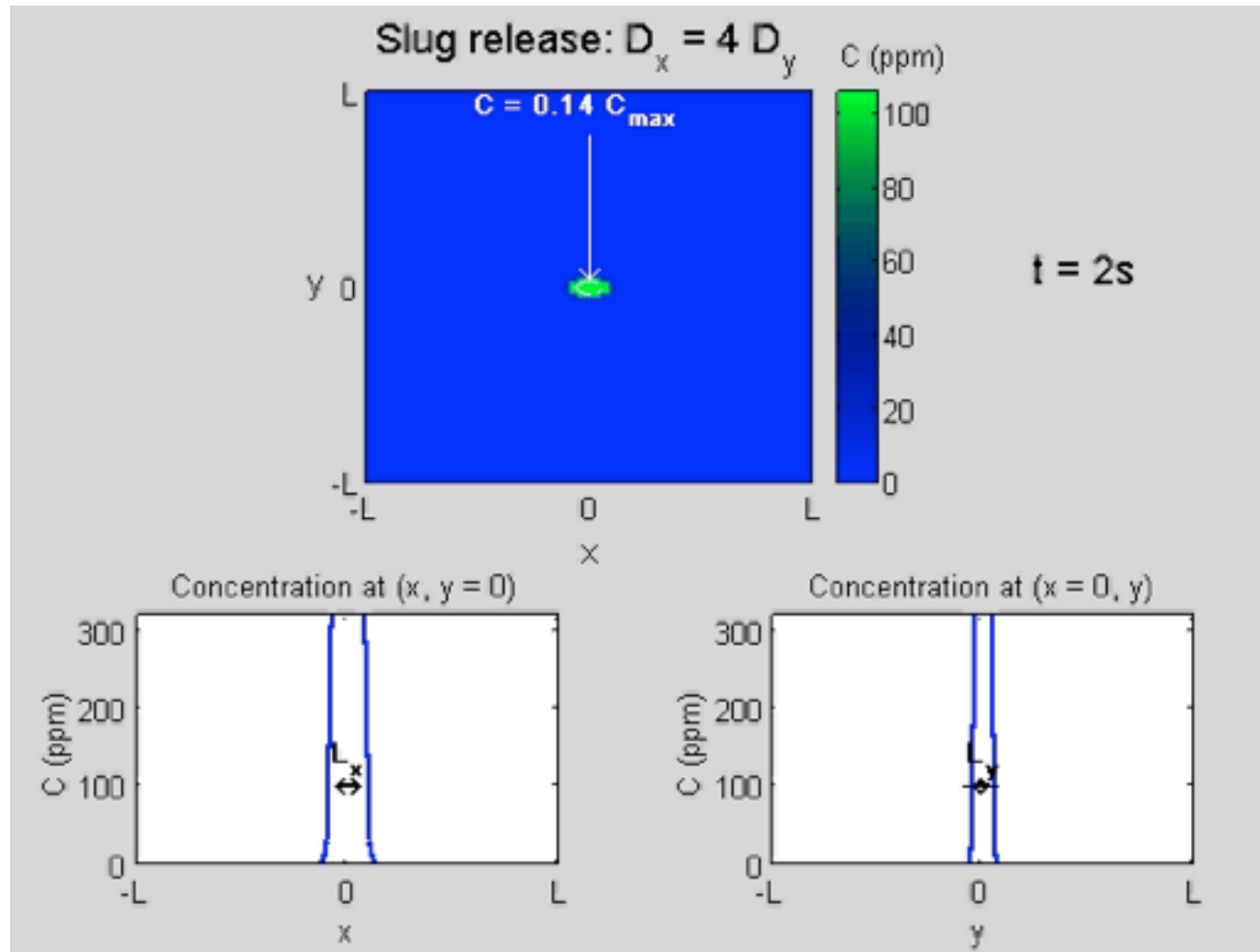
Norbert Wiener

(1894-1964)

MIT



Diffusion of an Instantaneous Point Source



This animation depicts the diffusion of a discrete mass released at $(x = 0, y = 0, t = 0)$. The diffusion is anisotropic, $D_x = 4 D_y$. The length scales grow in proportion to the square root of the diffusion, such that the dimensions of the cloud are anisotropic, with $L_x = 2 L_y$. Note that the profiles of concentration along the x - and y -axes are Gaussian in shape.