

March 29: Ivan Losev (MIT), “Quantization of nilpotent orbits vs. W -algebras.” ■

Let G be a semisimple algebraic group over \mathbb{C} , \mathfrak{g} its Lie algebra, and \mathbb{O} a nilpotent orbit in \mathfrak{g} . The goal of this talk is to relate quantizations of \mathbb{O} (and of its G -equivariant coverings) to one-dimensional modules over the W -algebra constructed from \mathbb{O} . By a quantization we mean a deformation quantization in the algebro-geometric setting equipped with some additional structures. The structures of interest are a G -action, a \mathbb{C}^\times -action and a quantum comoment map. The relationship is that, roughly, quantizations are in a natural (tautological in some sense) one-to-one correspondence with one-dimensional modules over the W -algebra.

To the speaker’s huge disappointment this result is not new, it was proved by Moeglin in the late 80s in a different but essentially equivalent form.

No prior knowledge of W -algebras is required.