"GEOMETRY OF DERIVED CATEGORIES AND REPRESENTATION THEORY" workshop schedule

Monday 4/30

9:30-10:30 – Okounkov, "Quantum cohomology of Nakajima varieties"

11-12 – Keller, "Combinatorial DT invariants and cluster algebras, I"

1:30-2:30 – Goncharov, "Ideal webs and moduli spaces of local systems on surfaces"

3:00-4:00 – Bayer, "Projectivity and birational geometry of Bridgeland moduli space"

Abstract: I will present a construction of a nef divisor class on moduli spaces of Bridgelandstable objects that is naturally associated to the stability condition. In the case of K3 surfaces, we use it to prove projectivity of the moduli spaces, thereby generalizing a recent result of Minamide, Yanagida and Yoshioka. The dependence of the divisor class on the stability condition gives a natural explanation for the correspondence between wall-crossing and birational geometry, as observed in examples Arcara-Bertram, Arcara-Bertram-Coskun-Huizenga and others. This is based on joint work with Emanuele Macri.

Tuesday 5/01

9:30-10:30 Keller, "Combinatorial DT invariants and cluster algebras, II"

11-12 Macri, "Bogomolov-Giesker inequality in higher dimension"

Abstract: In this seminar (based on joint work with A. Bayer, Y. Toda, and A. Bertram), we will present a conjectural approach to the construction of Bridgeland stability conditions on the derived category of a higher dimensional variety. The main ingredient is a generalization to complexes of the classical Bogomolov-Gieseker inequality for sheaves.

We will discuss several applications of this inequality. In particular, we will study the case of the 3-dimensional projective space and the connections with the Castelnuovo inequality for curves and the Fujita Conjecture.

1:30-2:30 Efimov, "Quantum cluster monomials via DT theory"

3:00-4:00 Kapranov, "Cubic relations in Hall algebras and zeroes of zeta functions."

4:15-5:15 – Gautam, "Yangians and quantum loop algebras".

Wednesday 5/02

9:30-10:30 Vasserot, "Affine W-algebras and quiver varieties."

10:45-11:45 Nagao, "Donaldson-Thomas theory and mapping class group"

Abstract: A 3-dimensional Calabi-Yau triangulated category may have non-trivial automorphism group. Such a symmetry is expected to provide some constraints in Donaldson-Thomas type theory for the category. In this talk, I will show an example of such a phenomenon.

Given a triangulation of a surface, a quiver with a potential is defined. Given a quiver with a potential, a 3-dimensional Calabi-Yau triangulated category (the derived category of GInzburg dga) is defined. The mapping class group of the original surface acts on the derived category. As a consequence, the Donaldson-Thomas theory is "invariant" under the mapping class group action.

1:15-2:15 Kamnitzer, "Quantizations of affine Grassmannian slices using subquotients of Yangians"

Abstract: We consider the slices to affine Schubert cells in the affine Grassmannian. These slices are Poisson varieties with a contracting \mathbb{C}^* action. They play an important role in the geometric Satake correspondence. We define a conjectural quantization of these slices using subquotients of Yangians. This is joint work with Webster, Weekes and Yacobi.

2:45-3:45 Seidel, "Mirror symmetry for A_m resolutions and smoothings"

2

Thursday

9:30-10:30 Cautis "Vertex operator constructions"

10:45-11:45 Shan, "Cyclotomic rational Cherednik algebras and affine Lie algebras"

1:15-2:15 Rouquier, "Perverse Equivalences, I"

2:45-3:45 Ginzburg, "The affine Grassmannian and symplectic geometry related to G/U."

Friday

9:30-10:30 Rouquier, "Perverse Equivalences, II"

10:45-11:45 Stroppel, "Generalized Kazhdan-Lusztig polynomials and completed Grothendieck groups"

1:15-2:15 Webster, "The representation theory of symplectic singularities."

2:45-3:45 Losev, "Highest weight categorical sl_2 -actions"

Abstract: We are going to discuss categorical actions of sl_2 on highest weight categories. We will mention structural results, applications to cyclotomic Rational Cherednik algebras and some open problems.