MIT \cdot 18.312 \cdot Spring 2013

PROBLEM SET 3 (additional problems)

Problem 18. Find and prove an explicit formula for the Y- Δ transformation of electrical networks.

Problem 19. For odd m and n, let B_1 be the $m \times n$ rectangle with a 1×1 square in position (1, 1) removed. Also let B_2 be the $m \times n$ rectangle with a 1×1 square in position (1, k) removed, where k is odd. Construct a bijection between domino tilings of B_1 and domino tilings of B_2 .

Problem 20. Consider an arrangement of n lines on the plane, where every pair of lines have one intersection point, and no 3 lines pass though the same point. Prove that where will be at least n-2 triangles amoung the regions on which the lines subdivide the plane.