

## Changes to text in printings 1-7 (Intro. to Analysis – Mattuck)

(Changes to Exercises, Problems, Questions and Answers are in a separate list.)

To determine Printing: Printing 3 has 10 9 8 7 6 5 4 3 on the first left-hand page, e.g. .

Printing 1 involves all the items below; Printing 2 only those starting with 2 or 3;

Printings 3-7 only those starting with 3. (Printing 8 incorporates all of them.)

**This list omits:** minor English typos, minor mathematical typos if judged not confusing.

(Printing 8 incorporates almost all of these too.)

**Bullets** mark the more significant small changes or corrections: missing or altered hypotheses, non-evident typos, new hints or simplifications; “line 5-” = fifth line from the bottom;

**Double Bullets** are used for more substantial additions or rewritings.

- 3 p. 10, Def. 1.6B: *read:* Any such  $C$
- 1 p. 52, Example 4.2, Solution: *change:*  $-u$  for  $u$  to:  $-u$  for  $a$ .
- 3 p. 55, line 7: *read:* if  $0 < |e_n| < .9$ ,
- 1 p. 55, line 11: *read:*  $e_0^4$
- 3 p. 57, display (17): *read:* if  $0 < |e_n| \leq .2$
- 3 p. 63, display (9): *delete:*  $> 0$
- 3 p. 63, line 11-: *read:*  $5.1/4$
- 1 p. 67, line 1: *read:* Example 5.2C
- 3 p. 68, line 10: *replace:* hypotheses *by:* symbols; *replace:* or *by:* and
- 3• p. 69, line 9: *read:* strictly increasing, clearly  $n_1 \geq 1, n_2 \geq 2$ , and so on, so eventually  
lines 11, 13: *replace:*  $i \gg 1$  *by:*  $i > N$
- 3 p. 73, line 2: *read:*  $a_n - L$
- 3 p. 73, line 6-: *read:* and estimate it: use 2.4(4), and (16a), suitably applied to  $\{b_n\}$ .
- 3 p. 82, Proof (line 2): *change:*  $a_n$  to  $x_n$
- 3 p. 95, display (6): *delete:*  $e$
- 1 p. 104, Display (12). *change:*  $f(n)$  to  $f(n+1)$ .
- 3 p. 104, line 10- *read:*  $N+1$
- 3 p. 106, line 10 *read:*  $\sum(-1)^{n+1}/n$
- 3 p. 107, line 2 *insert after* , : this follows by E-6.1/1b or E-5.41a, or reasoning directly,
- 3 p. 108, bottom half through top p.109 *replace everywhere:* “positive” and “negative”  
by “non-negative” and “non-positive” respectively
- 3 p. 114, line 3- *replace:*  $\leq$  *by*  $<$
- 3 p. 115, line 12- *read:*  $|a_n| < 1$
- 3 p. 121, line 9 *read:* 8.4A
  
- 3•• p. 122 *The proof given mislabels the two key sums in line 11, and doesn't show the absolute convergence of  $\sum c_n$ . Fix it by replacing line 12 with:*  
 $= d_n - e_n$ , where  $d_n$  and  $e_n$  are respectively the two positive series in the line above.  
*Then correct the rest by replacing everywhere  $c_n^+$  and  $c_n^-$  by  $d_n$  and  $e_n$  respectively.*  
  
*For the absolute convergence, insert the following before the final paragraph of the proof:*  
Since  $\sum d_n$  and  $\sum e_n$  are positive series, they are absolutely convergent, and  
$$\sum |c_n| = \sum |d_n - e_n| \leq \sum (|d_n| + |e_n|) = \sum d_n + \sum e_n,$$
which shows by the comparison theorem that  $\sum c_n$  is also absolutely convergent.
  
- 3• p. 143, Example 10.3A and Solution. *in*  $x^4 < x^2$ ,  $x^3 < x^2$  *replace*  $<$  *by*  $\leq$
- 3 p. 144, line 4- *read:* non-zero polynomial

3 p. 154, first line below pictures: *read*: points of discontinuity

3 p. 154, line 8 from bottom *insert paragraph*:

On the other hand, functions like the one in Exercise 11.5/4 which are discontinuous (i.e., not continuous) at every point of some interval are somewhat pathological and not generally useful in applications; in this book we won't refer to their  $x$ -values as points of discontinuity since "when everyone is somebody, then no one's anybody".

3 p. 156, line 4: *read*: In (8) below, the first limit exists if and only if the second and third exist and are equal;

3 p. 157, line 5: *read*:  $x \ll -1$

3 p. 161, line 11: *delete* ; , line 12: *read*  $<$ , line 13 *read*  $\leq$

3• p. 164, *read*:

**Thm. 11.4D'** Let  $x = g(t)$  and  $g(I) \subseteq J$ , where  $I$  is a  $t$ -interval,  $J$  an  $x$ -interval. Then  $g(t)$  continuous on  $I$  and  $f(x)$  continuous on  $J \Rightarrow f(g(t))$  continuous on  $I$ .

1• p. 166, Theorem 11.5A: *read*:  $\lim_{x \rightarrow a} f(x) = L$ . *read*:  $x_n \rightarrow a$ ,  $x_n \neq a$

1• p. 166, Theorem 11.5B: *read*:  $x_n \rightarrow a$ ,  $x_n \neq a$

3 p. 203, Theorem 14.3B: *label*: Local Extremum Theorem

3 p. 204, line 4: *read*: an open  $I$

2• p. 208, line 13: *replace by*: then show this limit is 0 and finish the argument using (b).

1 p. 208, line 19: *change fourteen to several*

3 p. 221, line 11- *read*:  $(a, b)$

3 p. 227, line 2: *read*:  $f'(x)$  not convex

3 p. 231, line 3- *change  $k$  to  $a$*

3 p. 235, display (15): *replace*:  $0 < |c| < |x|$  *by*:  $\begin{cases} 0 < c < x, \\ x < c < 0. \end{cases}$  *and delete next two lines*

1 p. 243, Example 18.2, Solution, lines 4 and 7 *read*:  $[0, x_1]$

3 p. 245 lines 1,2:  $f(x_{i-1})$ , line 15: two underscripts:  $[\Delta x_i]$

3•• p. 260, Defn. 19.6: *read*:  $a = x_0 < x_1 < \dots < x_{n-1} < x_n = b$ , *and add at end*:

and has finite left and right limits at each  $x_i$  (just a finite one-sided limit at  $x_0, x_n$ ).

(Thus  $f(x)$  can have discontinuities only at the  $x_i$ , and they are jump or removable.)

3• p. 261, Solution. *read*:

a)  $\tan x$  is piecewise monotone with respect to  $< 0, \pi/2, 3\pi/2, 2\pi >$ , but not piecewise continuous since its limits at  $\pi/2$  and  $3\pi/2$  are not finite.

(b) *read*:  $[1/(n+1)\pi, 1/n\pi]$

3 p. 261, Lemma 19.6 *rename*: Endpoint Lemma

3 p. 261, line 7- *replace*:  $[c, d]$  *by*  $[a, b]$

3 p. 273, line 2- : *read*: (cf. p. 271)

3 p. 282, line 2- : *read*: by interpreting the integral and limit geometrically

1 p. 294, line 6 from bottom: integral on the right is  $\int_{a^+}^b g(x) dx$

3 p. 307, Example 22.1C *read*: Show: as  $n \rightarrow \infty$ ,  $\frac{n}{1+nx}$

3 p. 310, Theorem 22.B *read*:  $\sum_0^\infty M_k$

1 p. 311, line 3-: *change 4 to 3b*

3 p. 316, Theorem 22.5A: *delete*: for all  $n \geq 0$

1 p. 331, line 3: *change 21.1c to 23.1Ac*

3 p. 332, middle *delete both*  $\aleph_1$ , *replace the third display by*:  $\aleph_0 = N(\mathbf{Z}) < N(S) < N(\mathbf{R})$

3 p. 335, lines 6-,7-: *read*: bounded and have only a finite number of jump discontinuities

3•• p. 340, replace last 9 lines of text before Questions 23.4 with the following:

Using Lebesgue integrals, simple versions of the Fundamental Theorems of Calculus are:

**Second Fundamental Theorem.** On  $I$ , if  $f(x)$  is L-integrable and  $F(x) = \int_a^x f(t) dt$ , then  $F'(x_0) = f(x_0)$  at any point  $x_0 \in I$  where  $f(x)$  is continuous.

**First Fundamental Theorem.**  $\int_a^b F'(x) dx = F(b) - F(a)$ , if  $F(x)$  is differentiable on  $[a, b]$  and  $F'(x)$  is L-integrable. (For both statements, there are versions with weaker hypotheses, which use the “almost everywhere” notion somewhere in the statement.)

3 p. 350, line 10-: *read:* Subsequence Theorem 5.4

3 p. 351, line 5-: *read:* infinite quarter-planes containing the  $x$ -axis and lying between

3• p. 353, line 4-: *read:* 24.4A;

3 line 2-: *read:*  $x + y = 2$

3 p. 354, Theorem 24.5B: *read:* for all  $\mathbf{x}_n$

3 line 7- *read:*  $f(\mathbf{x}_n)$

3 p. 357, Theorem 24.7B, line 2 *read:* non-empty compact set  $S$ ;

3 line 6 *read:* bounded and non-empty;

3 p. 367, line 15- *add:* Or make up a simple direct proof.

3 p. 369, Theorem 25.3A: (i) *read:* then  $S =$  ; (ii) *read:*  $S = \bigcup_{i \in I} U_i$

3 p. 377, Example 26.2B, Solution line 2: *read:*  $(-\infty, \infty)$  change (\*) to (5) throughout

3 p. 385, line 2- *read:*  $\int_0^1$

3•• p. 388, footnote: *read:* The first inequality in (7) is the analog, for absolutely convergent improper integrals, of the infinite triangle inequality for sums (E-7.3/1). Its proof goes::

For a fixed  $x$ , we have by the Absolute Value Theorem for integrals (19.4C)

$$\left| \int_R^S f(x, t) dt \right| \leq \int_R^S |f(x, t)| dt, \quad \text{for all } S > R, R \text{ fixed.}$$

As  $S \rightarrow \infty$ , the right side has the limit  $\int_R^\infty |f(x, t)| dt$ , since the integral  $\int_R^\infty f(x, t) dt$  is assumed to be absolutely convergent.

The left side has the limit  $|\int_R^\infty f(x, t) dt|$ , since the integral is convergent (by theorem 21.4), and  $||$  is a continuous function.

Finally, by the Limit Location Theorem 11.3C (21), the inequality is preserved as  $S \rightarrow \infty$ .

1 p. 391, Th. 27.4A line 2: *replace*  $I$  *by*  $[a, b]$

3 p. 399, line 18- *read:*  $a(b + c) = ab + ac$

3 p. 404, Example A.1C(i): *read:*  $a^2 + b^2 = c^2$

3•• p. 429 last 5 lines: *replace the sentences by:*

As the picture shows, since  $|f'(x)| > 1.2$  on  $[.7, 1]$ , its reciprocal  $|g'(x)|$  satisfies  $|g'(x)| < 1/1.2 \approx .8$  on the interval  $[0, f(.7)] = [0, .83]$ .

This shows Pic-2 is satisfied for  $g(x)$  on the interval  $[0, .83]$ ; the picture shows the root of  $x = g(x)$  will lie in this interval. Thus the Picard method can be used to solve  $x = g(x)$ . Starting with say .7, it leads to a root  $\approx .76$ .

3 p. 436, Remarks, first paragraph: *replace*  $x^3$  *by*  $x^4$

3 p. 439, top half: *change*  $p$  *and*  $q$  *to*  $P$  *and*  $Q$  (to avoid confusion with the use of the real number  $p$  in Example D.4)

3 p. 442, line 2: *read:*  $\geq$  line 6: *read:*  $\leq$

3 p. 459, ruler function: *read:* 169