Let $L$ be an exact Lagrangian submanifold of a cotangent bundle $T^*M$. If a topological obstruction vanishes, a Floer-theoretic construction of Nadler and Zaslow gives a functor from the category of local systems of $R$-modules on $L$ to the category of constructible sheaves of $R$-modules on $M$. I will discuss a variation of this construction that allows $R$ to be a ring spectrum. I hope it won’t take any knowledge of symplectic geometry to follow the talk. This is joint work with Xin Jin.