

# Topology Seminar

**Marc Hoyois**

of MIT will be speaking on

## The motivic Lefschetz fixed-point theorem

on October 6 at 4:30 in  
MIT Room 2-131

Let  $X$  be a smooth projective variety over the real numbers and let  $f : X \rightarrow X$  be a self-map. To  $X$  one can associate a real manifold  $X(\mathbb{R})$  and a complex manifold  $X(\mathbb{C})$ .  $l$ -adic cohomology gives a purely algebraic description of the Lefschetz number of  $f|_{X(\mathbb{C})}$ , but the Lefschetz number of  $f|_{X(\mathbb{R})}$  is invisible to  $l$ -adic cohomology. I will explain how the Lefschetz number of  $f|_{X(\mathbb{R})}$  is a motivic homotopy invariant and how a motivic version of the Lefschetz fixed-point formula for  $f$  subsumes the topological fixed-point formulas for  $f|_{X(\mathbb{C})}$  and  $f|_{X(\mathbb{R})}$ . I will then consider the situation over an abstract field and formulate an analogous refinement of the  $l$ -adic Grothendieck-Lefschetz trace formula.