

PHYSICAL MATHEMATICS SEMINAR

TOPIC: STRETCHING THE BOUNDARIES OF COMPUTATION:  
SELF-OPTIMIZING FFTS AND SEMI-ANALYTICAL  
APPROACHES IN ELECTROMAGNETISM

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ABSTRACT:

The recent surge of interest in the electromagnetism of nanostructured media, such as the periodic metamaterials known as photonic crystals, has invalidated many classical analytic approaches and led to increasing demands for computing power. In this talk, we discuss developments in two approaches to meeting such demands: semi-analytical methods, which dodge the bullet of brute force, and self-optimizing codes, which attack the speed problem head-on.

Some of the most challenging computational problems for brute-force methods involve the study of small effects in complex systems, such as the consequences of imperfections in a waveguide. The classical approach to such questions involves perturbation theory: given the solution for an idealized system, compute an analytical correction for small perturbations. Unfortunately, existing perturbative approaches, originally developed for the simple systems that were solvable decades ago, can fail completely in nano-structured media, due to the field discontinuities and rapid material variations in even the ideal system. Thus, it turns out that there are simple, general analytical questions in classical electromagnetism whose answer was unknown. We answer them, and in doing so extend many classical approaches, from perturbation theory to coupled-mode equations, to cover the new nano-structured regimes.

The other approach to large-scale computation demands has been the development of optimized software that extracts every ounce of speed from the available hardware. In particular, we focus on the case of the fast Fourier transform (FFT), an algorithm of particular importance in electromagnetism as well as in many other fields. We describe the development of FFTW, an FFT library that solves the problem of portable near-optimal performance by a combination of self-optimization, generation of computational kernels by a domain-specific "compiler", and "cache-oblivious" recursive algorithms. Unfortunately, we found that the approach that was prevalent until the early 1990's, that of minimizing the number of arithmetic operations, turns out to be largely irrelevant. Instead, we show how, in the latest release of FFTW, a wide variety of FFT algorithms can be expressed by a small number of composable recursive steps, allowing the FFTW runtime system to pick the algorithm that is fastest on any given hardware; the chosen algorithms are apparently unpredictable by simple heuristics.

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Refreshments at 3:30 PM in Building 2, Room 349.

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