

Introduction to Proofs
IAP 2015
In-class problems for day 4

Problem 7. Use mathematical induction to show that for every $n \in \mathbb{N}$, the quantity

$$(3 + \sqrt{5})^n + (3 - \sqrt{5})^n$$

is an even integer.

Proof.

□

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Problem 8. Let $(A_i : i \geq 1)$ be a sequence of countable sets. Show that

$$\bigcup_{i \in \mathbb{N} \setminus \{0\}} A_i$$

is also countable.

Proof.

□